

Adverse Selection in Insurance¹

Georges Dionne
HEC Montréal

Nathalie Fombaron
Université Paris Ouest

Wanda Mimra
ESCP Business School, Paris

November 30, 2023

¹ We thank Neil Doherty for his contribution to previous versions of this chapter and Claire Boisvert for her collaboration in preparing this version.

Abstract

In this survey we present some of the more significant results in the literature on adverse selection in insurance markets. Sections 1 and 2 introduce the subject, and Section 3 discusses the monopoly model developed by Stiglitz (1977) for the case of single-period contracts, which has been extended by many authors to the multi-period case. The introduction of multi-period contracts raises issues that are discussed in detail; time horizon, discounting, commitment of the parties, contract renegotiation, and accident underreporting. Section 4 covers the literature on competitive contracts, where the analysis is more complicated because insurance companies must take competitive pressures into account when they set incentive contracts. As pointed out by Rothschild and Stiglitz (1976), there is not necessarily a Nash equilibrium when there is adverse selection. However, market equilibrium can be sustained when principals anticipate competitive reactions to their behavior. Multi-period contracting is discussed. We show that different predictions on the evolution of insurer profits over time can be obtained from different assumptions concerning the sharing of information between insurers about an individual's choice of contracts and accident experience. The roles of commitment and renegotiation between the parties to the contract are important. Section 5 introduces models that consider moral hazard and adverse selection simultaneously, and Section 6 covers adverse selection when people can choose their risk status. Section 7 discusses many extensions to the basic models such as risk categorization, multidimensional adverse selection, symmetric imperfect information, double-sided adverse selection, participating contracts, and nonexclusive contracting.

Keywords: Adverse selection, insurance markets, monopoly, competitive contracts, self-selection mechanisms, single-period contracts, multi-period contracts, commitment, contract renegotiation, accident underreporting, risk categorization, participating contracts, nonexclusive contracting.

JEL Numbers: D80, D81, G22.

1 Introduction

In 1996, the European Group of Risk and Insurance Economists used its annual meeting to celebrate the 20th anniversary of the Rothschild and Stiglitz (1976) article “Equilibrium in Competitive Insurance Markets: An Essay in the Economics of Imperfect Information.” At this meeting, many papers on adverse selection were presented, and a subset of these presentations was published in a 1997 issue of the *Geneva Papers on Risk and Insurance Theory*. Another special issue on adverse selection was published in 2014 by the same journal (Muermann and Rothschild, 2014).

One of the articles in the first special issue was written by Rothschild and Stiglitz (1997) themselves. Their main topic was the role of competition in

insurance markets, with an emphasis on underwriting in a world with imperfect information. They argued that insurance competition using underwriting on preexisting conditions (such as genetic conditions) can limit the welfare benefits of insurance. In this survey, we concentrate on a subset of situations involving imperfect information in the insured-insurer relationship; we analyze situations of standard adverse selection where the insured has more information about his risk than the insurer. However, we will also consider extensions where insurers learn on individual characteristics that are not known by the insureds. We will also consider the assumption that risks are endogenous to individuals.

Adverse selection can be a significant resource allocation problem in many markets. In automobile insurance markets, risk classification is mainly explained by adverse selection (Dionne et al., 2001). In health insurance, different insurance policies or contracts are offered to obtain self-selection between different groups (Geruso and Layton, 2017). In life insurance, the screening of new clients through genetic tests is controversial and justified by asymmetric information between the insurer and the insured (Durnin et al., 2012). These three resource allocation mechanisms can be complements or substitutes, and adverse selection is not always a necessary condition for their presence. For example, in automobile insurance, we observe that insurers use risk classification and different deductible policies. Risk classification is usually justified by adverse selection, but the presence of different deductibles can also be explained by proportional transaction costs with different observable risks and by moral hazard. It is very difficult to verify whether or not the presence of different deductibles is justified by residual adverse selection. Another empirical test would be to verify whether bonus-malus schemes or multiperiod contracts with memory are explained in various markets by the presence of moral hazard, adverse selection, or both. We will not discuss these tests or these mechanisms in detail here; other contributions have addressed these issues (Chiappori and Salanié; 2013 and Dionne, 2013). Instead, we will review the major allocation mechanisms that can be justified by the presence of adverse selection. Emphasis will be placed on self-selection mechanisms in one-period contracting because much of the early literature was devoted to this subject (on risk classification, see Crocker et al., 2024). We will also discuss some extensions of these basic models; in particular, the role of multi-period contracting will be reviewed in detail. Finally, we will discuss the more recent contributions that focus on the effect of modifying the basic assumptions of the standard models. More specifically, we will see how introducing moral hazard in the basic Rothschild and Stiglitz (1976) model affects the conclusions about both the nature and the existence of an equilibrium. We will also introduce moral hazard in the monopoly model. Another subject will be insurance coverage when individuals can choose their risk status. Other extensions concern the consideration of multidimensional adverse selection (introduction of different risk-averse individuals or different privately known initial wealths combined with differences in risk, multiple risks), participating contracts, and the consideration of nonexclusive contracting. Our contribution does not cover in detail the normative and welfare aspects of adverse selection

in different markets, as two recent papers by Crocker (2023) and Rothschild (2023) review the main issues presented in the literature. This survey should be considered an update of Dionne et al. (2013a).²

2 Basic assumptions and some fundamental results

Without asymmetric information and under the standard assumptions of insurance models that we shall use in this article (same attitude toward risk and same risk aversion for all individuals in all classes of risk, one source of risk, risk neutrality on the supply side, no transaction cost in the supply of insurance, no learning and no moral hazard), a Pareto optimal solution is characterized by full insurance coverage for all individuals. Each insured sets his optimal consumption level according to his certain wealth. No other financial institution is required to obtain this level of welfare. Both risk categorization and self-selection mechanisms are redundant. There is no need for multi-period insurance contracts because they are not superior to a sequence of one-period contracts. Finally, the two standard theorems of welfare economics hold and market prices of insurance are equal to the corresponding social opportunity costs.

In insurance markets, adverse selection results from asymmetric information between the insured (agent) and the insurer (principal). The insureds are heterogeneous with respect to their expected loss and have more information than the insurance company which is unable to differentiate between risk types. Naturally, the high-risk individual has no incentive to reveal his true risk which is costly for the insurer to observe. Pooling of risks is often observed in insurance markets. “In fact, however, there is a tendency to equalize rather than to differentiate premiums... This constitutes, in effect, a redistribution of income from those with a low propensity of illness to those with a high propensity...” (Arrow, 1963; p. 964). One major difficulty is that a pooling cannot be a Nash equilibrium.

Akerlof (1970) showed that if all insurers have imperfect information on individual risks, an insurance market may not exist, or if it exists, it may not be efficient. He proposed an explanation of why, for example, people over 65 have great difficulty in buying medical insurance “the result is that the average medical condition of insurance applicants deteriorates as the price level rises — with the result that no insurance sales may take place at any price” (1970; p. 492). The seminal contributions of Akerlof and Arrow have generated a proliferation of

²For presentations of selection models in pictures under asymmetric information, see Einav and Finkelstein (2011) and Rothschild and Thistle (2022).

models on adverse selection. In this survey we shall, however, confine our attention to a limited subset. Many authors have proposed mechanisms to reduce the inefficiency associated with adverse selection, the “self-selection mechanism” in one-period contracts that induces policyholders to reveal hidden information by selection from a menu of contracts, (Rothschild and Stiglitz, 1976; Stiglitz, 1977; Wilson, 1977; Miyazaki, 1977; Spence, 1978; Hellwig, 1987, and the subsequent literature on the existence and characterization of equilibrium in competitive adverse selection markets), the “categorization of risks” (Hoy, 1982, 1989; Crocker and Snow, 1985, 1986, 1992; Dionne and Rothschild, 2014), and “multi-period contracting” (Dionne, 1983; Dionne and Lasserre, 1985, 1987; Kunreuther and Pauly, 1985; Cooper and Hayes, 1987; Hosios and Peters, 1989; Nilssen, 2000; Dionne and Doherty, 1994; Lund and Nilssen, 2004). All of them address private market mechanisms. In the first case, insurers offer a menu of policies with different prices and quantity levels so that different risk types choose different insurance policies. Pareto improvements for resource allocation with respect to the single-contract solution with an average premium to all clients can be obtained. In the second case, insurers use imperfect information to categorize risks and, under certain conditions, it is also possible to obtain Pareto improvements for resource allocation. In the third case, insurers use the information related to the past experience of the insured as a sorting device (i.e. to motivate high-risk individuals to reveal their true risk *ex ante*).

Before proceeding with the different models, let us comment briefly on some standard assumptions. We assume that all individuals maximize expected utility. The utility functions of the individuals in each risk group are identical, strictly concave and satisfy the von Neumann-Morgenstern axioms. Utility is time-independent, time-additive and state-independent. In many models there is no discounting but this is not a crucial issue.³ Individuals start each period with a given wealth, W , which is non-random. To avoid problems of bankruptcy, the value of the risky asset is lower than W . All risks in the individual’s portfolio are assumed to be insurable. Income received in a given period is consumed in that period; in other words, there is no saving and no banking or lending. Insurers are risk neutral and maximize the value of their cash flows or profits. Insurers can enforce exclusive insurance contracts and there are no transaction costs in the supply of insurance. Finally, the insureds are assumed to be unable to influence either the probabilities of accident or the damages due to accidents; this rules out any problem of moral hazard.

To simplify the presentation we explicitly assume that insurers are risk neutral. An equivalent assumption is that insurers are well diversified in the sense that much of their total risk is diversified by their own equity holders in the management of their personal portfolios. The presence of transaction costs would not affect the qualitative conclusions concerning the effects of adverse selection on resource allocation in insurance markets (see Dionne et al., 1999, for more

³Some aspects of the discounting issues are discussed in Section 3.

details). However, proportional transaction costs (or proportional loadings) are sufficient to explain partial insurance coverage and their explicit introduction in the analysis would modify some conclusions in the reference models. For example, each individual in each class of risk would buy less than full insurance in the presence of full information and the introduction of adverse selection will further decrease the optimal coverage for the low-risk individuals. Consequently the presence of adverse selection is not a necessary condition to obtain different deductibles in insurance markets.

The presence of many sources of non-insurable risks or of many risky assets in individual portfolios is another empirical fact that is not considered in the models. As long as these risks are independent, the conclusions should not be affected significantly. However, the optimal portfolio and insurance decisions in the presence of many correlated risks and asymmetric information in one or in many markets is still an open question in the literature.

In reality, we observe that banks coexist with insurers that offer multi-period insurance contracts. The presence of saving and banking may change the conclusions obtained for multi-period contracts under asymmetric information. Particularly, it may modify accident reporting strategies and commitment to the contracts. However, with few exceptions (Allen, 1985, moral hazard; Dionne and Lasserre, 1987, adverse selection; Fudenberg et al., 1986, moral hazard; Caillaud et al., 2000, insurance and debt with moral hazard), research on principal-agent relationships has not envisaged the simultaneous presence of several alternative types of assets and institutions (see Chiappori et al., 1994, for detailed discussion of different issues related to the effect of savings on the optimality of multi-period contracts).

There remain the assumptions on the utility function. Although the theory of decision making under uncertainty has been challenged since its formal introduction by von Neumann and Morgenstern (Machina, 1987, 2000), it has produced very useful analytical tools for the study of optimal contracts such as optimal insurance coverage and the associated comparative statics, and the design of optimal contracts under moral hazard or the characterization of optimal insurance policies under adverse selection.

While there is by now an abundant literature on non-EU models, very few of these have addressed the adverse selection problem. In this survey we thus limit the discussion to the linear expected utility model. We also assume that utility functions are not function of the states of the world and that all individuals in all classes of risks have the same level of risk aversion. As we will see, some of these assumptions are not necessary to get the desired results but permit the discussion to focus on differences in the risk types.

3 Monopoly

3.1 Public information

There are two possible states of the world ($x \in \{n, a\}$); state (n), "no accident" having the probability $(1 - p_i)$ and state (a), "accident" having the probability $0 < p_i < 1$. Consumers differ only by their probability of accident. For simplicity, there are two types of risk in the economy ($i \in \{H, L\}$ for High and Low-risk) with $p_H > p_L$. Each consumer owns a risky asset with monetary value $D(x)$; $D(a) = 0$ in state (a) and $D(n) = D$ in state (n). Therefore the expected loss for a consumer of type i ($E_i D(x)$) is $p_i D$.

Under public information and without transaction cost, a risk neutral private monopoly⁴ would offer insurance coverage (net of premium) (β_i) for an insurance premium (α_i) such that a consumer will be indifferent between purchasing the policy and having no insurance (Stiglitz, 1977). In other words, the private monopolist maximizes his total profit over α_i , β_i and λ_i :

Problem 1

$$\text{Max}_{\alpha_i, \beta_i, \lambda_i} \sum q_i ((1 - p_i) \alpha_i - p_i \beta_i) \quad (1)$$

under the individual rationality (or participating) constraints⁵

$$V(C_i | p_i) - V(C^0 | p_i) \geq 0 \quad i = H, L \quad (2)$$

where $V(C_i | p_i)$ is the expected utility under the contract $C_i = \{\alpha_i, \beta_i\}$;

$$V(C_i | p_i) = p_i U(W - D + \beta_i) + (1 - p_i) U(W - \alpha_i);$$

$U(\cdot)$ is a twice differentiable, strictly increasing and strictly concave function of final wealth ($U'(\cdot) > 0, U''(\cdot) < 0$);

W is non-random initial wealth;

C^0 denotes no insurance; $C^0 = \{0, 0\}$ and

$V(C^0 | p_i) \equiv p_i U(W - D) + (1 - p_i) U(W)$; $V(C^0 | p_i)$ is the reservation utility.

q_i is the number of policies sold to consumers of type i ;

λ_i is a Lagrangian multiplier for constraint (2).

⁴For an analysis of several reasons why a monopoly behavior in insurance markets should be considered, see Dahlby (1987). For examples of markets with a monopoly insurer see D'Arcy and Doherty (1990) and Dionne and Vanasse (1992).

⁵For a detailed analysis of participation constraints, see Jullien (2000).

It is well known that full insurance, $\beta_i^* = D - \alpha_i^*$ (for $i = H, L$), is the solution to the above problem and that (2) is binding for both classes of risk, which means that

$$V(C_i^* | p_i) = V(C^0 | p_i) \quad i = H, L$$

or

$$\alpha_i^* = p_i D + z_i^*,$$

where z_i^* is the maximum unit-profit (or the Arrow-Pratt risk premium) on each policy. In other words z_i^* solves $U(W - p_i D - z_i^*) = p_i U(W - D) + (1 - p_i)U(W)$.

The private monopoly extracts the entire consumer surplus. However, there is no efficiency cost associated with the presence of a monopoly because each individual buys full insurance as under perfect competition⁶. This is the classical result that Pareto efficient risk sharing between a risk-averse agent and a risk-neutral principal shifts all the risk to the principal. To sum up we can write:

Proposition 1 *In the presence of public information about insureds' underlying risk, an optimal contract between a private monopolist and any individual of type i is characterized by:*

- a) full insurance coverage, $\beta_i^* = D - \alpha_i^*$;
- b) no consumer surplus, $V(C_i^* | p_i) = V(C^0 | p_i)$.

Both solutions are shown at C_H^* and C_L^* in Figure 1 where C^0 is the “initial endowment” situation and where the vertical axis is wealth in the accident or loss state and the horizontal axis is wealth in the no-loss state.

Insert Figure 1 here.

Any point to the northwest of C^0 and below or on the 45° degree line represents the wealth of the insured with any contract where $\alpha_i \geq 0$ and $\beta_i \geq 0$. Because the monopoly solution implies no consumer surplus, it must lie on each risk type indifference curve passing through C^0 . These indifference curves are strictly convex because $U(\cdot)$ is strictly concave by assumption.⁷

⁶As in the perfect discrimination case, the monopolist charges a price of insurance to each consumer equal to marginal cost. All potential consumer surplus is collected as monopoly profits so there is no dead weight loss. This result would not be obtained with a proportional loading.

⁷Since individuals of different types have the same degree of risk aversion, at each point in the figure, the absolute value of the slope of the high-risk indifference curve is lower than that of the low-risk individual. For example at point C^0 , $U'(W)(1 - p_H)/U'(W - D)p_H < U'(W)(1 - p_L)/U'(W - D)p_L$. At equilibrium points C_H^* and C_L^* , the respective slopes (in absolute values) are $(1 - p_H)/p_H$ and $(1 - p_L)/p_L$. This is true because under full insurance, the insured of type i has $W - p_i D - z_i^*$ in each state.

3.2 Private information and single-period contracts

Under private information the insurer does not observe the individual's risk types⁸, and must introduce mechanisms to ensure that agents will reveal this characteristic. Stiglitz (1977) extended the Rothschild-Stiglitz (1976) model to the monopoly case. In both contributions, price-quantity contracts⁹ permit the separation of risks by introducing incentives for individuals to reveal their type. Low-risk individuals reveal their identity by purchasing a policy that offers limited coverage at a low unit price. Thus they trade off insurance protection to signal their identity. Formally, risk revelation is obtained by adding two self-selection constraints to Problem 1:

$$V(C_i | p_i) - V(C_j | p_i) \geq 0 \quad \begin{array}{l} i, j = H, L \\ i \neq j \end{array} \quad (3)$$

Equation (3) guarantees that individual i prefers C_i to C_j . Let us use λ_{HL} and λ_{LH} for the corresponding Lagrangian multipliers where λ_{HL} is for the self-selection constraint of the H type risk and λ_{LH} is that for the L type. λ_{HL} and λ_{LH} cannot both be positive.¹⁰ From Figure 1 it is easy to observe that, if the high-risk individuals are indifferent between both contracts ($\lambda_{HL} > 0$), the low-risk individuals will strictly prefer their own contracts ($\lambda_{LH} = 0$). Moreover, λ_{LH} cannot be positive when λ_{HL} is zero because this leads to a violation of (2). Therefore, a feasible solution can be obtained only when $\lambda_{HL} > 0$ and $\lambda_{LH} = 0$.

Figure 1 shows the solution to the maximization of (1) subject to (2) and (3) where low-risk individuals choose a positive quantity of insurance¹¹ $\beta_L^{**} > 0$ and high-risk individuals buy full insurance coverage ($\beta_H^{**} = \beta_H^*$). Separation of risks and profit maximization imply that $V(C_H^{**} | p_H) = V(C_L^{**} | p_H)$. As discussed above, it is clear that (2) and (3) cannot both be binding for the high-risk individuals when it is possible for the low-risks to buy insurance. In fact, Figure 1 indicates that C_H^{**} is strictly preferred to C_H^* which means that high-risk individuals get some consumer surplus when the monopolist sells insurance

⁸For models where neither the insurer nor the insured know the individuals' probabilities of accident, see Palfrey and Spatt (1985), Maluq (1988), Boyer et al. (1989), and De Garidel-Thoron (2005).

⁹We limit our discussion to private market mechanisms. On public provision of insurance and adverse selection, see Pauly (1974) and Dahlby (1981).

¹⁰Technically the preference structure of the model implies that indifference curves of individuals with different risks cross only once. This single crossing property has been used often in the sorting literature (Cooper, 1984).

¹¹There is always a separating equilibrium in the monopoly case. However, the good-risk individuals may not have any insurance coverage at the equilibrium. Property 4 in Stiglitz (1977) establishes that $C_L^{**} = \{0, 0\}$ when q_H/q_L exceeds a critical ratio of high to low-risk individuals where q_i is the proportion of individuals i in the economy. The magnitude of the critical ratio is function of the difference in accident probabilities and of the size of the damage. Here, to have $C_L^{**} \neq \{0, 0\}$, we assume that q_H/q_L is below the critical ratio.

to the low-risk individuals. In other words, the participation constraint (2) is not binding for the H individuals ($\lambda_H = 0$).

Another property of the solution is that good risk individuals do not receive any consumer surplus ($\lambda_L > 0$). However, as discussed above, they strictly prefer their contract to the contract offered to the bad risk individuals. In other words

$$V(C_L^{**} | p_L) = V(C^0 | p_L) \quad \text{and} \quad V(C_L^{**} | p_L) > V(C_H^{**} | p_L),$$

which means that the self-selection constraint is not binding for the low-risk individuals unlike the participation constraint.

In conclusion, one-period contracts with a self-selection mechanism increase the monopoly profits under private information compared with a single contract without any revelation mechanism, but do not necessarily correspond to the best risk allocation arrangement under asymmetric information. In particular, good risk individuals may not be able to buy any insurance coverage or, if they can, they are restricted to partial insurance. As we shall see in the next section, multi-period contracts can be used to relax the binding constraints and to improve resource allocation under asymmetric information. In summary

Proposition 2 *In the presence of private information, an optimal one-period contract menu between a private monopoly and individuals of types H and L has the following characteristics:*

- a) $\beta_H^{**} = D - \alpha_H^{**}; \beta_L^{**} < D - \alpha_L^{**}$
- b) $V(C_H^{**} | p_H) > V(C^0 | p_H); V(C_L^{**} | p_L) = V(C^0 | p_L)$
- c) $V(C_H^{**} | p_H) = V(C_L^{**} | p_H); V(C_L^{**} | p_L) > V(C_H^{**} | p_L)$.

Proof. See Stiglitz (1977). ■

Stiglitz (1977) also considered a continuum of agent types and showed that some of the above results can be obtained under additional conditions. Chade and Schlee (2012) revisit the monopolist insurer problem. For an arbitrary type distribution¹², they extend all of the known results for the two-type case: the highest risk type gets full coverage (efficiency at the top), all other types get less than full coverage, the premium and coverage are nonnegative for all types and co-monotone and the insurer makes positive expected profit (there are always gains to trade).¹³ Chade and Schlee (2012) also derive conditions under which the monopolist insurer can offer global quantity discounts, a result that is not found in competitive insurance market.

Kong *et al.* (2023) show how subsidies reduce competition between insurers under adverse selection and can create un-natural monopoly.

¹²that doesn't include the type $p = 1$.

¹³Chade and Schlee (2020) introduce insurance provision cost into the monopoly insurance model and find that the introduction of insurance costs can imply no gains of trade for the highest risks. Furthermore, complete pooling is possible.

3.3 Multi-period insurance contracts

Multi-period contracts are often observed in different markets. For example, in many countries, drivers buy automobile insurance with the same insurer for many years and insurers use bonus-malus systems (or experience rating) to relate insurance premiums to the individual’s past experience (Lemaire, 1985; Henriot and Rochet, 1986; Hey, 1985; Dionne and Vanasse, 1989, 1992, and Dionne *et al.* 2013). Long term contracting is also observed in labor markets, workers’ compensation insurance, service contracts, unemployment insurance and many other markets. The introduction of multi-period contracts in the analysis gives rise to many issues such as time horizon, discounting, commitment of the parties, myopic behavior, accident underreporting, and contract renegotiation. These issues are discussed in the following paragraphs.

Multi-period contracts are set not only to adjust ex-post insurance premiums or insurance coverage to past experience, but also as a sorting device. They can be a complement or a substitute to standard self-selection mechanisms. However, in the presence of full commitment, ex-ante risk announcement or risk revelation remains necessary to obtain optimal contracts under adverse selection.

In Cooper and Hayes (1987), multi-period contracts are presented as a complement to one-period self-selection constraints. Because imperfect information reduces the monopolist’s profits, the latter has an incentive to relax the remaining binding constraints by introducing contracts based on anticipated experience over time. By using price-quantity contracts and full commitment in long term contracts, Cooper and Hayes introduce a second instrument to induce self-selection and increase monopoly profits: experience rating increases the cost to high-risks from masquerading as low-risks by exposing them to second-period contingent coverages and premia.

Cooper and Hayes’ model opens with a direct extension of the standard one-period contract presented above to a two-period world with full commitment on the terms of the contract. There is no discounting and all agents are able to anticipate the values of the relevant futures variables. To increase profits, the monopolist offers contracts in which premiums and coverages in the second period are function of accident history in the first period. Accidents are public information in their model. The two period contract C_i^2 is defined by:

$$C_i^2 = \{\alpha_i, \beta_i, \alpha_{ia}, \beta_{ia}, \alpha_{in}, \beta_{in}\}$$

where a and n mean “accident” and “no accident” in the first period and where α_{il} and β_{il} ($l = a, n$) are “contingent” choice variables. Conditional on accident experience, the formal problem consists of maximizing two-period expected profits by choosing C_L^2 and C_H^2 under the following constraints:

$$V(C_i^2 | p_i) \geq 2V(C^0 | p_i) \tag{4.1}$$

$$V(C_i^2 | p_i) \geq V(C_j^2 | p_i) \quad \begin{array}{l} i, j = H, L \\ i \neq j \end{array} \quad (4.2)$$

where

$$\begin{aligned} V(C_i^2 | p_k) \equiv & p_k U(W - D + \beta_i) + (1 - p_k) U(W - \alpha_i) \\ & + p_k [p_k U(W - D + \beta_{ia}) + (1 - p_k) U(W - \alpha_{ia})] \\ & + (1 - p_k) [p_k U(W - D + \beta_{in}) + (1 - p_k) U(W - \alpha_{in})] \\ & k = i, j \quad i, j = H, L \quad i \neq j. \end{aligned}$$

The above constraints show that agents are committed to the contracts for the two periods. In other words, the model does not allow the parties to renegotiate the contract at the end of the first period. Moreover, the principal is committed to a loss-related adjustment of the insurance contract in the second period negotiated at the beginning of the first period. The insured is committed, for the second period, to buy the coverage and to pay the premium chosen at the beginning of the first period. It is also interesting to observe from (4) that the decisions concerning insurance coverage in each period depend on the anticipated variations in the premiums over time. In other words, (4) establishes that variations in both premia and coverages in the second period are function of experience in the first period. Using the above model, Cooper and Hayes proved the following result:

Proposition 3 *In the presence of private information and full commitment, the monopoly increases its profits by offering an optimal two-period contract having the following characteristics :*

1) *High-risk individuals obtain full insurance coverage in each period and are not experience rated*

$$\hat{\alpha}_H = \hat{\alpha}_{Hn} = \hat{\alpha}_{Ha}, \quad \hat{\beta}_H = \hat{\beta}_{Ha} = \hat{\beta}_{Hn}$$

where $\hat{\beta}_H = D - \hat{\alpha}_H$

2) *Low-risk individuals obtain partial insurance with experience rating*

$$\hat{\alpha}_{Ln} < \hat{\alpha}_L < \hat{\alpha}_{La}, \quad \hat{\beta}_{La} < \hat{\beta}_L < \hat{\beta}_{Ln}$$

3) *Low-risk individuals do not obtain any consumer surplus, and high-risk individuals are indifferent between the two contracts*

$$\begin{aligned} V(\hat{C}_L^2 | p_L) &= 2V(C^0 | p_L), \\ V(\hat{C}_H^2 | p_H) &= V(\hat{C}_L^2 | p_H). \end{aligned}$$

Proof. See Cooper and Hayes (1987). ■

The authors also discuss an extension of their two-period model to the case where the length of the contract may be extended to many periods. They show that the same qualitative results as those in Proposition 3 hold with many periods.

Dionne (1983) and Dionne and Lasserre (1985, 1987) also investigated multi-period contracts in the presence of both adverse selection¹⁴ and full commitment by the insurer. Their models differ from that of Cooper and Hayes (1987) in many respects. The main differences concern the revelation mechanism, the sorting device, commitment assumptions and the consideration of statistical information. Moreover, accidents are private information in their models. Unlike Cooper and Hayes (1987), Dionne (1983) did not introduce self-selection constraints to obtain risk revelation. Instead risk revelation results from a Stackelberg game where the insurer offers a contract in which the individual has to select an initial premium by making a risk announcement in the first period. Any agent who claims to be a low-risk pays a corresponding low premium as long as his average loss is less than the expected loss given his declaration (plus a statistical margin of error to which we shall return). If that condition is not met, he is offered a penalty premium. Over time, the insurer records the agent's claims and offers to reinstate the policy at the low premium whenever the claims frequency become reasonable again.¹⁵

Following Dionne (1983) and Dionne and Lasserre (1985), the no-claims discount strategy consists in offering two full insurance premiums¹⁶ ($F^1 = \{\alpha_H, \alpha_L\}$) in the first period and for $t = 1, 2, \dots$

$$F^{t+1} \begin{cases} = \alpha_d \text{ if } \sum_{s=1}^{N(t)} \theta^s / N(t) < E_d D(x) + \delta_d^{N(t)} \\ = \alpha_k \text{ otherwise} \end{cases}$$

where

α_d is the full information premium corresponding to the declaration (d),
 $d \in \{H, L\}$

θ^s is the amount of loss in contract period s , $\theta^s \in \{0, D\}$

α_k is a penalty premium. α_k is such that $U(W - \alpha_k) < V(C_0 | p_H)$

$E_d D(x)$ is the expected loss corresponding to the announcement (d)

$\delta_d^{N(t)}$ is the statistical margin of error

¹⁴Townsend (1982) discussed multi-period borrowing-lending schemes. However, his mechanism implies a constant transfer in the last period that is incompatible with insurance in the presence of private information.

¹⁵This type of "no-claims discount" strategy was first proposed by Radner (1981) and Rubinstein and Yaari (1983) for the problem of moral hazard (see also Malueg (1986) where the "good faith" strategy is employed). However, because the two problems of information differ significantly the models are not identical. First the information here does not concern the action of the agent (moral hazard) but the type of risk which he represents (adverse selection). Second, because the action of the insured does not affect the random events, the sequence of damage levels is not controlled by the insured. The damage function depends only on the risk type. Third, in the adverse selection model, the insured cannot change his declaration and therefore cannot depart from his initial risk announcement although he can always cancel his contract. Therefore, the stronger conditions used by Radner (1981) (robust epsilon equilibrium) and Rubinstein and Yaari (1983) ("long proof") are not needed to obtain the desired results in the presence of adverse selection only. The Law of the Iterated logarithm is sufficient.

¹⁶In fact their formal analysis is with a continuum of risk types.

$N(t)$ is the total number of periods with insurance; $N(t) \leq t$.

Therefore, from the construction of the model, $\sum_{s=1}^{N(t)} \theta^s / N(t)$ is the average loss claimed by the insured in the first $N(t)$ periods. If this number is strictly less than the declared expected loss plus some margin of error, the insurer offers α_d . Otherwise he offers α_k . The statistical margin of error is used to avoid penalizing honest insureds too often. Yet it has to be small enough to detect those who try to increase their utility by announcing a risk class inferior to their true risk. From the Law of the Iterated Logarithm, one can show that

$$\delta_d^{N(t)} = \sqrt{2\gamma\sigma_d^2 \log \log N(t)/N(t)}, \quad \gamma > 1$$

where σ_d^2 is the variance of the individual's loss corresponding to the declaration (d) and $\delta_d^{N(t)}$ converges to zero over time (with arbitrary large values for $N(t)$).

Graphically, we can represent $E_d D(x) + \delta_d^{N(t)}$ in the following way:

Insert Figure 2 here.

As $N(t) \rightarrow \infty$, $E_d D(x) + \delta_d^{N(t)} \rightarrow E_d D(x)$.

Over time, only a finite number of points representing $(\sum \theta^s / N(t))$ will have a value outside the shaded area.

Proposition 4 below shows that the full information allocation of risks is obtainable using the no-claims discount strategy as $T \rightarrow \infty$ and as long as the agents do not discount the future.¹⁷

Proposition 4 *Let individual of type i be such that:*

$$\alpha_i - E_i D(x) \geq 0 \text{ and } U(W - \alpha_i) \geq V(C^0 | p_i).$$

Then, when $T \rightarrow \infty$, there exists a pair of optimal strategies for the individual of type i and the private monopoly having the following properties:

1) the strategy of the monopoly is a "no-claims discount strategy"; the strategy of insured i is to tell the truth about his type in period 1 and to buy insurance in each period;

2) the optimal corresponding payoffs are $\alpha_i^ - E_i D(x) = z_i^*$ and $U(W - \alpha_i^*) = V(C^0 | p_i)$, $i = H, L$;*

3) both strategies are enforceable.

¹⁷In general, introducing discounting in repeated games reduces the incentives of telling the truth and introduces inefficiency because players do not care for the future as they care for the current period. In other words, with discounting, players become less patient and cooperation becomes more difficult to obtain. See Sabourian (1989) and Abreu et al. (1990) for detailed discussions of the discount factor issues in repeated contracts.

Proof. See Dionne and Lasserre (1985). ■

It is also possible to obtain a solution close to the public information allocation of risks in finite horizon insurance contracts. Dionne and Lasserre (1987) show how a trigger strategy with revisions¹⁸ may establish the existence of an ε equilibrium. This concept of ε equilibrium is due to Radner (1981) and was also developed in the moral hazard context. Extending the definition to the adverse selection problem, Dionne and Lasserre (1987) defined an ε equilibrium as a triplet of strategies (principal, low-risk individual, high-risk individual) such that, under these strategies, the expected utility of any one agent is at least equal to his expected utility under public information less epsilon. In fact, the expected utility of the high-risk individual is that of the full information equilibrium.

As for the case of an infinite number of periods,¹⁹ Dionne and Lasserre (1987) showed that it is in the interest of the monopolist (which obtains higher profits) to seek risk revelation by the insured rather than simply use the ex-post statistical instrument to discriminate between low-risk and high-risk agents. In other words, their second main result shows that it is optimal to use statistical tools not only to adjust, ex-post, insurance premiums according to past experience, but also, to provide an incentive for the insured to announce, ex-ante, the true class of risk he represents. Finally, they conclude that a multi-period contract with announcement dominates a repetition of one-period self-selection mechanisms (Stiglitz, 1977) when the number of periods is sufficiently large and there is no discounting. This result contrasts with those in the economic literature where it is shown that the welfare under full commitment is equal to that corresponding to a repetition of one-period contracts. Here, a multiperiod contract introduces a supplementary instrument (experience rating) that increases efficiency (Dionne and Doherty, 1994; Dionne and Fluet, 2000).

Another characteristic of Dionne and Lasserre's (1987) model is that low-risk agents do not have complete insurance coverage when the number of periods is finite; they chose not to insure if they are unlucky enough to be considered as high-risk individuals. However, they always choose to be insured in the first period and most of them obtain full insurance in each period. Finally, it must be pointed out that the introduction of a continuum of agent types does not

¹⁸Radner's (1981) contribution does not allow for revisions after the initial trigger. However, revisions were always present in infinite horizon models [Rubinstein and Yaari (1983), Dionne (1983), Radner (1985), Dionne and Lasserre (1985)]. A trigger strategy without revision consists in offering a premium corresponding to a risk declaration as long as the average loss is less than the reasonable average loss corresponding to the declaration. If that condition is not met, a penalty premium is offered for the remaining number of periods. With revisions, the initial policy can be reinstate.

¹⁹See also Gal and Landsberger (1988) on small sample properties of experience rating insurance contracts in the presence of adverse selection. In their model, all insureds buy the same contracts, and experience is considered in the premium structure only. They show that the monopoly's expected profits are higher if based on contracts that take advantage of longer experience.

create any difficulty in the sense that full separation of risks is obtained without any additional condition.

In Dionne (1983) and Dionne and Lasserre (1985) there is no incentive for accident underreporting at equilibrium because there is no benefit associated with underreporting. When the true classes of risk are announced, insureds cannot obtain any premium reduction by underreporting accidents. When the number of periods is finite, matters are less simple because each period matters. In some circumstances, the insured has to evaluate the trade-off between increased premiums in the future and no coverage in the present. This is true even when the contract involves full commitment as in Dionne and Lasserre (1987). For example, the unlucky good risk may prefer to receive no insurance coverage during a particular period to pass a trigger date and have the opportunity to pay the full information premium as long as his average loss is less than the reasonable average loss corresponding to his class of risk.

We now address the incentive for policyholders to underreport accidents. The benefits of underreporting can be shown to be nil in a two-period model with full commitment and no statistical instrument when the contract cannot be renegotiated over time. To see this, let us go back to the two-period model presented earlier (Cooper and Hayes, 1987) and assume that accidents are now private information. When there is *ex ante* full commitment by the two parties to the contract one can write a contract where the net benefit to any type of agent from underreporting is zero. High-risk individuals have full insurance and no experience rating at equilibrium and low-risk individuals have the same level of expected utility whatever the accident reporting at the end of the second period. However, private information about accidents reduces insurers' profits compared with the situation where accidents are public information.

In all the preceding discussions it was assumed that the insurer can precommit to the contract over time. It was shown that an optimal contract under full commitment can be interpreted as a single transaction where the incentive constraints are modified to improve insurance possibilities for the low-risk individuals and to increase profits. Because there is full commitment and no renegotiation, accident histories are uninformative on the risk type. This form of commitment is optimal in Dionne (1983) and Dionne and Lasserre (1985): as in the Arrow-Debreu world, neither party to the contract can gain from renegotiation. However, in a finite horizon world, the role of renegotiation becomes important because self-selection in the first period implies that future contracts might be inefficient given the public information available after the initial period. When the good risks have completely revealed their type, it becomes advantageous to both parties – the insurer and the low-risk individuals – to renegotiate a full insurance contract for the second period. Although the possibilities of renegotiation improve welfare in the second period, they violate the *ex-ante* self-selection constraints and reduce *ex-ante* welfare. In other words, renegotiation limits the commitment possibilities and reduces parties' welfare

ex-ante. For example, if the high-risk individuals anticipate renegotiation in the second period, they will not necessarily reveal their type in the first period (Dionne and Doherty, 1994).

Formally, we can interpret the possibility of renegotiation as adding a new constraint to the set of feasible contracts; unless parties can precommit to not renegotiate then contracts must be incentive compatible and renegotiation-proof (Dewatripont, 1989; Bolton, 1990; Rey and Salanié, 1996). To reduce the possibilities of renegotiation in the second period, the insurer that cannot commit not to renegotiate after new information is revealed must set the contracts so that the insured type will not be perfectly known after the first period. This implies that the prospect of renegotiation reduces the speed of information revelation over time. In other words, the prospect of renegotiation can never improve the long term contract possibilities. In many circumstances, a sequence of one-period contracts will give the same outcome as a renegotiated-proof long term contract; in other circumstances a renegotiation-proof long-term contract dominates (when intertemporal and intertype transfers and experience rating are allowed, for example) (Hart and Tirole, 1988; Laffont and Tirole, 1987, 1990, 1993; Dionne and Doherty 1994; see the next section for more details).

Hosios and Peters (1989) present a formal model that rules out any renegotiation by assuming that only one-period contracts are enforceable.²⁰ They also discuss the possibility of renegotiation in the second period when this renegotiation is beneficial to both parties. Although they cannot show the nature of the equilibrium under this alternative formally, they obtain interesting qualitative results. For example, when the equilibrium contract corresponds to incomplete risk revelation in the first period, the seller offers, in the second period, a choice of contract that depends on the experience of the first period. Therefore accident underreporting is possible without commitment and renegotiation. This result is similar to that obtained in their formal model where they ruled out any form of commitment for contracts that last for more than one period. Only one-period contracts are enforceable. They show the following results.²¹

Proposition 5 *In absence of any form of commitment from both parties to the contract:*

²⁰On limited commitment see also Freixas et al. (1985), Laffont and Tirole (1987) and Dionne and Fluet (2000).

²¹However, separating equilibria are possible with discounting because future considerations are less relevant. In a model with commitment and renegotiation, Dionne and Doherty (1994) obtain a similar result; when the discount factor is very low a separating equilibrium is always optimal in a two-period framework. Intuitively, low discount factors reduce the efficiency of using intertemporal transfers or rents to increase the optimal insurance coverage of the low-risk individuals by pooling in the first period. See Laffont and Tirole (1993) for a general discussion on the effect of discounting on optimal solutions in procurement when there is no uncertainty. See Dionne and Fluet (2000) for a demonstration that full pooling can be an optimal solution when the discount factor is sufficiently high and when there is no commitment. This result is due to the fact that, under no-commitment, the possibilities of rent transfers between the periods are limited.

1) *Without discounting, separating equilibria do not exist; only pooling and semi-separating equilibria are possible.*

2) *Accident underreporting can now affect the seller's posterior beliefs about risk types and insurance buyers may fail to report accidents to avoid premium increases.*

Proof. See Hosios and Peters (1989). ■

This result implies that the insurer does not have full information on the risk types at the end of the first period; therefore, accidents reports become informative on the risk type contrary to the Cooper and Hayes (1987) model. However, the authors did not discuss the optimality of such two-period contract. It is not clear that a sequence of one-period contracts with separating equilibrium does not dominate their sequence of contracts.

Contrary to the theoretical literature on insurance where risk types are permanent over time, Farinha Luz (2022) characterizes multi-period insurance contracts where the probability distribution over losses (determining the risk-type good or bad and privately known by the consumer) follows a Markov process. Types are persistent over time, in the sense that having a given type in period t leads to a higher probability of having the same type in period $t+1$.

Like in Dionne and Doherty (1994), in each period, the current insurer has access to two sources of information : accident report and the consumer's contract choice. A no claim and the choice of partial coverage in a given period are rewarded with more attractive contracts in subsequent periods. Optimal contracts under full commitment offer a choice between an experience-rated partial coverage policy where future offers are depending on additional realizations and a perpetual complete coverage policy with fixed premium in each period. Because of the correlation in types over time, the efficient way to reward good type (without inducing misreports by bad type agents) is by rewarding the consumer whenever he remains a good type.

In a monopolistic setting, the optimal menu of contracts with commitment is always separating. The policyholder with an initial good type has no informational rent (his intertemporal expected utility is the same as the one he would have if he did not insure) while the policyholder with an initial bad type receives an informational rent under the condition that an initial bad type is unlikely²² (his intertemporal expected utility is greater than that of the no-insurance option).

See also Battaglini (2005) for long-term contracting in monopoly setting with Markovian consumers in the case of linear consumption utility.

²²This condition is close to that existing in a context of static monopoly according to which bad risks obtain a rent from the insurer if the frequency ratio q_H/q_L is sufficiently low (Property 4 in Stiglitz 1977).

4 Competitive contracts

We now introduce a competitive context. Competition raises many new issues in both static and dynamic environments. The two main issues that will be discussed here are 1) the choice of an adequate equilibrium concept and the study of its existence and efficiency properties, and 2) the nature of information between competitive insurers (and consequently the role of government in facilitating the transmission of information between insurance market participants, particularly in long-term relationships).

In a first step, the situation where no asymmetric information affects the insurance market is presented as a benchmark. After that, issues raised by the adverse selection problem and the remedies to circumvent it are discussed.

4.1 Public information about an individual's characteristics

In a competitive market where insurance firms are able to discriminate among the consumers according to their riskiness, we would expect insureds to be offered a menu of policies with a complete coverage among which they choose the one that corresponds with their intrinsic risk. Indeed, under competition, firms are now constrained to earn zero expected profits. When information on individual risk characteristics is public, each firm knows the risk type of each individual. The optimal individual contract is the solution to:

Problem 2

$$\underset{\alpha_i, \beta_i, \lambda_i}{Max} p_i U(W - D + \beta_i) + (1 - p_i) U(W - \alpha_i) + \lambda_i [(1 - p_i)\alpha_i - p_i\beta_i], \quad i = H, L$$

where $(1 - p_i)\alpha_i = p_i\beta_i$ is the zero-profit constraint.

As for the monopoly case under public information, the solution to Problem 2 yields full insurance coverage for each type of risk. However, contrary to a monopoly, the optimal solutions C_H^* and C_L^* in Figure 3 correspond to levels of consumer welfare greater than in the no-insurance situation (C^0). As already pointed out, the monopoly solution under public information also yields full insurance coverage and does not introduce any distortion in risk allocation. The difference between the monopoly and competitive cases is that in the former, consumer surplus is extracted by the insurer, while in the latter it is retained by both types of policyholder.

Under competition, a zero-profit line passes through C^0 and represents the set of policies for which a type i consumer's expected costs are nil for insurers.

The value of its slope is equal to the (absolute) ratio $\frac{1-p_i}{p_i}$. Each point on the segment $[C^0 C_i^*]$ has the same expected wealth for an individual of type i than that corresponding to C^0 . The full information solutions are obtained when the ratio of slopes of indifference curves is just equal to the ratio of the probability of not having an accident to that of having an accident. To sum up,

Proposition 6 *In an insurance world of public information about insureds' riskiness, a one-period optimal contract between any competitive firm on market and any individual of type i ($i = H, L$) is characterized by:*

- a) *full insurance coverage, $\beta_i^* = D - \alpha_i^*$*
- b) *no firm makes a surplus, $\pi(C_i^* | p_i) = 0$*
- c) *consumers receive a surplus $V(C_i^* | p_i) > V(C^0 | p_i)$.*

Characteristic b) expresses the fact that premiums are set to marginal costs and characteristic c) explains why individual participation constraints (2) are automatically satisfied in a competitive context. Consequently, introducing competitive actuarial insurance eliminates the wealth variance at the same mean or corresponds to a *mean preserving contraction*.

Insert Figure 3 here.

Under perfect information, competition leads to one-period solutions that are *first-best efficient*. This result does not hold when we introduce asymmetric information.

4.2 Private information and single-period contracts

In the presence of adverse selection, the introduction of competition may lead to fundamental problems with the existence and the efficiency of an equilibrium. When insurance firms cannot distinguish among different risk types, they lose money by offering the set of full information contracts (C_H^*, C_L^*) described above, because both types will select C_L^* (the latter contract requires a premium lower than C_H^* and in counterpart, also fully covers the incurring losses). Each insurer will make losses because the average cost is greater than the premium of C_L^* , which is the expected cost of group L. Under asymmetric information, traditional full information contracts to allocate risk optimally are not feasible. Consequently, many authors have investigated the role of sorting devices in a competitive environment to circumvent this problem of adverse selection. The first contributions on the subject in competitive markets are by Akerlof (1970), Pauly (1974), Rothschild and Stiglitz (1976) and Wilson (1977). The literature on competitive markets is now very large; it is not our intention here to review all contributions. We will focus on the contributions particularly relevant to the study of insurance markets.

A first distinction that we can make is between models of signaling (informed agents move first) and of screening (uninformed agents move first) (Stiglitz and Weiss, 1984). Spence (1973) and Cho and Kreps (1987) models are of the first type and are mainly applied to labor markets in which the workers (informed agents) move first by choosing an education level (signal). Then employers bid for the services of the workers and the latter select the more preferred bids. Cho and Kreps (1987) present conditions under which this three-stage game generates a Riley (1979) single-period separating equilibrium.²³ Without restrictions (or criteria such as those proposed by Cho and Kreps (1987)) on out-of-equilibrium beliefs, many equilibria arise simultaneously, which limit the explanatory power of the traditional signaling models considerably.²⁴ Although it may be possible to find interpretations of the signaling models in insurance markets, it is generally accepted that the screening interpretation is more natural. Rothschild and Stiglitz (1976) and Wilson (1977) introduced insurance models of screening.

Let us start with the Rothschild and Stiglitz (1976) model. Uninformed insurers offers contracts to individuals privately informed about their risk type, who choose among the contracts. Each insurer knows the proportions of high-risk and low-risk individuals in the market but has no information on an individual's type. Moreover, each insured cannot, by assumption, buy insurance from several insurers. Otherwise, the individual insurers would not be able to observe the individuals' total amount of insurance and would not be able to discriminate easily.²⁵ Finally, an insurer only needs to observe the claims he receives.²⁶

Rothschild and Stiglitz (1976) define equilibrium in a competitive insurance market as a set of contracts such that, when customers choose contracts to maximize expected utility, (i) no contract in the equilibrium set makes negative expected profits; and (ii) there is no contract outside the equilibrium set that, if offered, will make a nonnegative profit. This notion of equilibrium is of the Cournot-Nash type, the equilibrium allocations are those of Nash equilibria of a screening game in which insurers simultaneously offer contracts in a first stage

²³A Riley or reactive equilibrium leads to the Rothschild-Stiglitz separating equilibrium regardless of the number of individuals in each class of risk.

²⁴Multiple equilibria are the rule in two-stage signaling models. However, when such equilibria are studied, the problem is to find at least one that is stable and dominates in terms of welfare. For a more detailed analysis of signaling models see the survey by Kreps (1989). On the notion of sequential equilibrium and on the importance of consistency in beliefs see Kreps and Wilson (1982).

²⁵Jaynes (1978) and Hellwig (1988) analyze the consequences of relaxing this assumption. Specifically, they specify the conditions under which an equilibrium exists under nonexclusive contracting when the sharing of information about customers is treated endogenously as part of the game among firms. We discuss Jaynes (1978) and Hellwig (1988) in more detail in Section 7 on nonexclusive contracting and firm communication.

²⁶This is a consequence of the exclusivity assumption. Because we consider static contracts, observing accidents or claims does not matter. This conclusion will not necessarily be true in dynamic models.

and customers choose a contract in the second stage. Rothschild and Stiglitz obtained three significant results:

Proposition 7 *In the Rothschild-Stiglitz competitive insurance market*

- a) *A pooling equilibrium is not possible; the only possible equilibria are with the separating Rothschild-Stiglitz allocation.*
- b) *The Rothschild-Stiglitz allocation is not necessarily second-best efficient.*
- c) *A separating equilibrium may not exist.*

A pooling equilibrium is an equilibrium in which both types of risk buy the same contract. The publicly observable proportions of good-risk and bad-risk individuals are respectively q_L and q_H (with $q_H + q_L = 1$) and the average probability of having an accident is \bar{p} . This corresponds to line C^0F in Figure 4a. To see why pooling cannot be sustained in equilibrium, assume that C_1 in the figure is a pooling equilibrium contract for a given insurer. By definition, it corresponds to zero aggregate expected profits; otherwise, another insurer in the market will offer another pooling contract. Because of the relative slopes of the risk type indifference curves, there always exists a contract C_2 that will be preferred to contract C_1 by the low-risk individuals, and that yields positive profits to the insurer offering it when taken out by the low risks. This is called a 'cream-skimming' deviation. Consequently, equilibrium cannot be pooling.

Insert Figure 4a here.

Insert Figure 4b here.

To find the candidate separating equilibrium contracts, the formal solution can be obtained by adding to Problem 2 the self-selection constraints that guarantee that individual i prefers C_i to C_j . By a similar argumentation to the one used in the determination of the optimal solution in the monopoly situation, it can be shown that only the self-selection constraint of the high-risk type is binding. Furthermore, competition ensures that the high-risk type receives full insurance, and cross-subsidization of high-risk types is not possible due to cream-skimming deviations. The nonnegative profit constraint is thus binding on each type so the problem is limited to finding an optimal contract for the low-risk individual as follows:

Problem 3

$$\underset{\alpha_L, \beta_L, \lambda_L, \lambda_{HL}}{\text{Max}} \quad p_L U(W - D + \beta_L) + (1 - p_L) U(W - \alpha_L)$$

subject to the zero-profit constraints

$$(1 - p_i) \alpha_i = p_i \beta_i$$

and the (high-risk) self-selection constraint

$$U(W - \alpha_H^{**}) = p_H U(W - D + \beta_L) + (1 - p_H) U(W - \alpha_L).$$

High-risk individuals receive full insurance ($\alpha_H^{**} = \alpha_H^* = D - \beta_H^*$) because the low-risk self-selection constraint is not binding. The solution of Problem 3 implies that the low-risk type receives less than full insurance.²⁷ We can summarize the description of the candidate separating equilibrium contracts, known as the Rothschild-Stiglitz contracts, with the following proposition:

Proposition 8 *In the presence of private information, the candidate separating equilibrium one-period contracts, the Rothschild-Stiglitz contracts, have the following characteristics:*

- a) $\beta_H^{**} = D - \alpha_H^{**}$; $\beta_L^{**} < D - \alpha_L^{**}$
- b) $V(C_i^{**} | p_i) > V(C^0 | p_i) \quad i = H, L$
- c) $V(C_H^{**} | p_H) = V(C_L^{**} | p_H)$; $V(C_L^{**} | p_L) > V(C_H^{**} | p_L)$.
- d) $\alpha_H^{**} = p_H D$, $(1 - p_L)\alpha_L^{**} = p_L \beta_L^{**}$

Figure 4b shows the Rothschild-Stiglitz allocation. High-risk individuals buy full insurance (C_H^{**}), while low-risk individuals get only partial insurance C_L^{**} .²⁸ Each firm earns zero expected profit on each contract. This allocation has the advantage for the low-risk agents that their premium corresponds to their actuarial risk and does not contain any subsidy to the high-risk individuals. However, a cost is borne by low-risk insureds in that their contract delivers only partial insurance compared with full insurance in the full information case. Only high-risk individuals receive the first-best allocation.

An important observation is that the Rothschild-Stiglitz contracts do not depend on the shares of high-risk and low-risk individuals in the population. Indeed, as high-risk individuals receive full insurance at their actuarially-fair premium, the low-risk contract is fully pinned down by the high-risk type incentive constraint (preferences) and the zero-profit constraint on low-risks (low-risk loss probability). Cross-subsidization between the risk types is ruled out.²⁹ This highlights that the Rothschild-Stiglitz contracts are not necessarily second-best efficient. An allocation is second-best efficient if it is Pareto-optimal within the set of allocations that are feasible and the zero-profit constraint on the portfolio.³⁰ When the share of high risks is low, the expected utility of both risk types could be improved by a pooling contract or menu that provides the low risks with more insurance and the high risks with a lower, subsidized premium. Low-risk

²⁷Partial coverage is generally interpreted as a monetary deductible. However, in many insurance markets the insurance coverage is excluded during a probationary period that can be interpreted as a sorting device. Fluet (1992) analyzed the selection of an optimal time-deductible in the presence of adverse selection.

²⁸On the relationship between the coverage obtained by a low-risk individual under monopoly compared to that under competition see Dahlby (1987). It is shown, for example, that under constant absolute risk aversion, the coverage obtained by a low-risk individual under monopoly is greater than, equal to, or less than that obtained under competition because the monopolist's expected profit on a policy purchased by low-risk individuals is greater than, equal to, or less than its expected profit on the policy purchased by high-risk individuals.

²⁹By definition of equilibrium in Rothschild and Stiglitz (1976) and by the problem of cream-skimming deviations in the game-theoretic version.

³⁰See Crocker and Snow (1985, 1986) for more details.

individuals receive a higher expected utility than from their Rothschild-Stiglitz contract if the costs of subsidizing high-risks are low (low q_H).

The third important result from Rothschild and Stiglitz (1976), directly related to the above discussion on efficiency-improving pooling/cross-subsidization, is that there are conditions under which a separating equilibrium does not exist. In general, equilibrium does not exist if the costs of pooling are low for the low-risk individuals (few high-risk individuals or low q_H , which is not the case in Figure 4b because the line C^0F' corresponds to a value of q_H higher than the critical level q_H^{RS} permitting separating equilibria³¹) or if the costs of separating are high (structure of preference). In the former case, given the separating RS contracts, the cost of sorting (partial insurance) exceeds the benefits (no subsidy). Then, a profitable pooling deviation by an insurer exist. As already discussed, however, pooling cannot be an equilibrium.

In Rothschild and Stiglitz (1976) as well as most of the subsequent work, there are only two risk types. Riley (1979) shows that the existence problem is severe with a continuum of risk types.³² In more recent work, Hendren (2014) clarifies the relationship between Rothschild and Stiglitz unravelling (competitive Nash equilibrium does not exist) and Akerlof unravelling (competitive Nash equilibrium of no trade) in the baseline screening game: when the type distribution contains a continuous interval or includes $p = 1$, either there is a competitive Nash equilibrium of no trade (Akerlof unravelling) or a Competitive (Nash) Equilibrium does not exist (Rothschild and Stiglitz unravelling). The condition for existence (but without trade) is that no one is willing to pay the pooled cost of worse risks in order to obtain some insurance.³³

The original equilibrium non-existence result from Rothschild and Stiglitz (1976) has prompted a large literature modelling competitive (insurance) markets with adverse selection, given that many insurance markets function even in the presence of adverse selection. To date, there is however still not an agreed upon model of equilibrium in competitive adverse selection insurance markets. In the following, we will review and structure the main strands of the literature.

One extension is to consider a mixed strategy in which an insurer's strategy is a probability distribution over a menu of contracts. Rosenthal and Weiss (1984) show that a separating Nash equilibrium always exists when the insurers adopt this strategy. Farinha Luz (2017) provides a characterization in the game-theoretic formulation of Rothschild and Stiglitz (1976) with contract menus and

³¹The critical share of high-risks for a separating equilibrium to exist is lower when insurers offer only single contracts (as in the main part of Rothschild and Stiglitz, 1976) than when an insurer can offer contract menus.

³²The problem is that there is a profitable local deviation at the higher endpoint (at the highest risk) of the distribution.

³³Hendren (2013) derives this no trade condition in an insurance market with an endogenous set of contracts. This helps to explain insurance rejections based on observable, high-risk characteristics, as these groups might be too adversely selected.

shows that the mixed equilibrium features cross-subsidization across risk levels, dependence of offers on the risk distribution and price dispersion generated by firm randomization over offers. However, it is not clear that such a strategy has any particular economic interpretation in insurance markets unlike in many other markets.³⁴

An important observation is that in a competitive market, insurers might react to competitors, in particular insurers might want to modify their own contract offers in reaction to competitors' contract offers. In the works of Wilson (1977) and Riley (1979), this idea was translated into new equilibrium concepts that include expectations about competitor behavior. Subsequent work (e.g. Hellwig 1987; Engers and Fernandez 1987; Asheim and Nilssen 1996; Netzer and Scheuer 2014; Mimra and Wambach 2019a) explicitly models dynamic strategic interaction in competitive insurance markets.

Regarding new equilibrium concepts, Riley (1979)'s reactive equilibrium notion incorporates an expectation rule that firms add new contracts in reactions to entrants/new contract offers. The Riley equilibrium always implements the separating Rothschild-Stiglitz allocation.³⁵ The logic is that insurers would expect that following a pooling deviation that upsets the candidate separating equilibrium in Rothschild and Stiglitz (1976), other insurers could add cream-skimming contracts, which would render the pooling attempt unprofitable.

In contrast to expectations of new contracts being added, Wilson (1977) proposes the anticipatory equilibrium concept, which is based on an expectation rule that (unprofitable) contracts will be withdrawn. A set of contracts is a Wilson equilibrium if (1) each contract in the equilibrium set makes nonnegative profits and (2) there is no new set of contracts which earns nonnegative profits for each contract and strictly positive profit for some new contract after the contracts in the original set which have become unprofitable are withdrawn. A Wilson equilibrium always exists, it either implements the Rothschild-Stiglitz allocation or a pooling allocation in which low-risk type utility is maximized subject to an aggregate zero-profit condition (Wilson pooling contract, C_1 in Figure 4a.) Pooling is possible in the Wilson equilibrium as the expectation of unprofitable contracts being withdrawn prevents cream-skimming deviations: Everybody would expect contract C_1 in Figure 4a to be withdrawn if, for instance, contract C_2 in Figure 4a were offered by some insurers. This would render C_2 which would then attract not only low risks but also high risks, unprofitable.³⁶

³⁴See also Dasgupta and Maskin (1986) and Rothschild and Stiglitz (1997). On randomization to improve market functioning in the presence of adverse selection see Garella (1989) and Arnott and Stiglitz (1988).

³⁵Engers and Fernandez (1987) generalize Riley (1979)'s reactive equilibrium notion. Azevedo and Gottlieb (2019) give an example that shows that a Riley equilibrium may not exist if consumers are not ordered.

³⁶See Grossman (1979) for an analysis of the Wilson type equilibrium with reactions of insureds rather than reactions of sellers.

Wilson also considers subsidization between policies, but Miyazaki (1977) and Spence (1978) develop the idea more fully. They show how to improve welfare of both classes of risk (or of all n classes of risk; Spence, 1978) with the low-risk class subsidizing the high-risk class. Spence shows that, in a model in which firms react (in the sense of Wilson) by dropping loss-making policies, an equilibrium always exists. In all the above models, each of the contracts in the menu is defined to permit the low-risk policyholders to signal their true risk. The resulting equilibrium is a break-even portfolio of separating contracts, and exists regardless of the relative value of q_H . The separating solution has no subsidy between policies when $q_H \geq q_H^{WMS}$. More formally we have

Proposition 9 *A Wilson-Miyazaki-Spence (WMS) equilibrium exists regardless of the value of q_H . When $q_H \geq q_H^{WMS}$, the WMS equilibrium allocation corresponds to the Rothschild-Stiglitz allocation. When $q_H < q_H^{WMS}$, high-risks are cross-subsidized in equilibrium.*

The WMS equilibrium (C_3, C_4) is illustrated in Figure 5 for the case of two risk classes with cross-subsidization from the low to the high-risk group. The curve denoted by *frontier* in Figure 5 is the zero aggregate transfers locus defined such that the contract pairs yield balanced transfers between the risk-types, and the subset (C_3, Z) in bold is the set of contracts for the low-risk individuals that are second-best efficient. The derivation of the optimal contracts with transfers is obtained by maximizing the following program:

Problem 4

$$\underset{\alpha_L, \beta_L, t, s}{Max} \quad p_L U(W - D + \beta_L - t) + (1 - p_L) U(W - \alpha_L - t)$$

subject to the non-negative aggregate profit constraint

$$q_L t \geq q_H s$$

the zero-profit constraint before cross-subsidization

$$(1 - p_L) \alpha_L \geq p_L \beta_L$$

the self-selection constraint

$$U(W - \alpha_H^{**} + s) \geq p_H U(W - D + \beta_L - t) + (1 - p_H) U(W - \alpha_L - t)$$

the positivity constraint

$$s \geq 0$$

where s and t are for subsidy and tax respectively.

When the positivity constraint is binding, (C_3, C_4) corresponds to the Rothschild-Stiglitz contracts (C_H^{**}, C_L^{**}) without cross-subsidization. When the positivity

constraint holds with a strict inequality, the equilibrium involves subsidization from low-risks to high-risks.³⁷

The Wilson-Miyazaki-Spence (WMS) equilibrium (C_3, C_4) solves this program if (C_3, C_4) is second-best efficient in the sense of Harris and Townsend (1981).³⁸ In competitive insurance markets, Crocker and Snow (1985) prove the following proposition, which can be seen as an analogue with the welfare first theorem (Henriet and Rochet, 1986):

Proposition 10 *A Wilson-Miyazaki-Spence (WMS) equilibrium is second-best efficient for all values of q_H .*

Proof. See Crocker and Snow (1985).

Subsidization between different risk classes is of special interest for characterizing the notion of second-best optimality and simultaneously the shape of optimal redistribution in insurance markets. Indeed, the optimal allocation on these markets (given the incentive constraints imposed by adverse selection) involves cross-subsidization between risk types. Thus, the *second-best efficient* contracts resulting from this redistribution are described for low-risk individuals by the frontier in bold in Figure 5 (see Crocker and Snow, 1985).

It can be shown that the Rothschild and Stiglitz allocation is second-best efficient if and only if q_H is higher than some critical value q_H^{WMS} .³⁹ The same problem applies to the Riley equilibrium as it sustains the Rothschild and Stiglitz solution regardless of the value of q_H . In the income-states space, the shape of this curve can be convex as shown in Figure 5 (Dionne and Fombaron, 1996) under some unrestrictive assumptions about utility functions. More precisely, some conditions about risk aversion and prudence indexes guarantee the strict convexity of the efficiency frontier: the insurance coverage β_L offered to low-risks is a convex function in the subscribed premium α_L . High-risks are offered a coverage β_H which is a linear function in the premium α_H . It is shown by Dionne and Fombaron (1996) that this frontier can never be strictly concave under risk aversion. At least a portion of the frontier must be convex.⁴⁰

Insert Figure 5 here.

³⁷For a proof that the equilibrium can never imply subsidization from high-risk individuals to low-risk individuals, see Crocker and Snow (1985).

³⁸See Lacker and Weinberg (1999) for a proof that a Wilson allocation is coalition proof.

³⁹On the relationship between risk aversion and the critical proportion of high-risks so that the Rothschild and Stiglitz allocation is second-best efficient, see Crocker and Snow (2008). Their analysis shows that, when the utility function U becomes more risk averse, the critical value of high-risks increases if U exhibits nonincreasing absolute risk aversion.

⁴⁰For more general utility functions, the curvature can be both convex and concave in the premium but must necessarily be convex around the full insurance allocation under risk aversion. For more details, see Pannequin (1992) and Dionne and Fombaron (1996).

Despite the presence of non-convexities of this locus in the income-states space, the correspondence between optimality and market equilibrium is maintained (see Prescott and Townsend, 1984, for a general proof of this assertion, and Henriot and Rochet, 1986, for an analysis in an insurance context). Consequently, the conventional question about the possibility of achieving a second-best efficient allocation by a decentralized market does not arise. An analogue to the second optimality theorem holds for an informationally constrained insurance market (Henriot and Rochet, 1986): even though government cannot a priori impose risk-discriminating taxes on individuals, it can impose a tax on their contracts and thus generate the same effect as if taxing individuals directly (Crocker and Snow, 1986).

Gemmo et al. (2020) prove the existence of the WMS equilibrium in models with continuous one-dimensional type spaces under general assumptions about preferences, and provide an efficient algorithm for computing it for quasilinear preferences. Their work highlights that the (quantitative) welfare implications of public policies such as a coverage mandate critically hinge on whether the market implements a constrained efficient allocation like the WMS equilibrium or a constrained inefficient allocation of the Rothschild-Stiglitz form.

While the above discussion presented new equilibrium concepts, notably the Wilson anticipatory equilibrium, and discussed efficiency properties, another strand of the literature models dynamic strategic interaction in competitive insurance markets. Some of these in particular present game-theoretic modelling for the reactive and anticipatory equilibrium concepts. As pointed out early by Hellwig (1987), the conclusions from this literature are very sensitive to subtle details of the game specification.

Engers and Fernandez (1987) provide a game-theoretic foundation for Riley's (1979a) reactive equilibrium. They propose the following game: First, insurers set contract menus. After observation of competitors' offers, firms may repeatedly add new contracts to their existing contracts and this stage ends endogenously when no firm wants to add contracts anymore. After this stage, consumers choose contracts. This implements the Riley logic such that an equilibrium with the Rothschild-Stiglitz allocation exists. However, different allocations can be sustained as equilibrium allocations as well.⁴¹

Hellwig (1986, 1987) introduces a three-stage game in which the insurer may reject in the third stage the insured's contract choice made in the second stage. Hellwig (1986, 1987) shows that the Wilson pooling contract may correspond to a sequential equilibrium of the three-stage game. The basic logic is that if

⁴¹Mimra and Wambach (2016) embed the Riley logic in a dynamic set-up where consumers arrive on the market during the contract offer stages. They show that with these active consumers purchasing contracts during the contract offer stages the RS/Riley allocation is the unique equilibrium allocation.

an insurer attempts to cream-skim, the other insurers would reject the (high-risk) applicants for their contracts, which would be anticipated by (high-risk) consumers who would then also apply for the deviating contract. Contrary to the Rothschild and Stiglitz two-stage model, the three-stage game always has a sequential equilibrium in pure strategies. The most plausible sequential equilibrium is pooling rather than sorting whenever pooling is Pareto preferred.⁴²

Another way of introducing some form of dynamics in a non-cooperative model is renegotiation in Asheim and Nilssen (1996). Their model allows insurers to make a second move after having observed the contracts that their applicants initially sign, under the restriction that this renegotiation is non-discriminating (a contract menu offered by an insurer to one of its customers has to be offered to all its customers). Such non-discriminating renegotiation weakens the profitability of cream-skimming, to the extent that the unique (renegotiation-proof) equilibrium of the game is the WMS outcome.

In contrast, Inderst and Wambach (2001) solve the equilibrium non-existence problem by considering firms which face capacity constraints (due to limited capital for instance).⁴³ Under the constraint that no single insurer can serve the whole market, each customer receives in equilibrium her Rothschild-Stiglitz contract. The main intuition is that a pooling deviation would be unprofitable, as the gain in utility at this deviating contract is higher for high-risk individuals due to the single-crossing property, who are thus prepared to accept a higher (expected) rationing probability than low-risk types leading to a bad risk selection. However, the equilibrium is not unique.

In the last decade, there has been renewed interest in competitive insurance markets with adverse selection. Netzer and Scheuer (2014) consider market exit by firms after initial contract offers have been observed and allow firms to offer any finite set of contracts so that cross-subsidization is not ruled out. They show that the Wilson-Miyazaki-Spence contracts are the unique equilibrium outcome with small withdrawal costs. Mimra and Wambach (2019a) present a model of individual contract withdrawals that captures the strategic process underlying Wilson (1977)'s anticipatory equilibrium concept and show that an equilibrium exists with the WMS allocation. However, this equilibrium requires latent contracts on offer.

Diasakos and Koufopoulos (2018) modify the game in Hellwig (1987) along two dimensions. First, firms can offer contract menus, and second, they can choose to publicly pre-commit upon the future delivery of their menus. They

⁴²While in a three-stage game in signaling models (Cho and Kreps, 1987) it is the pooling rather than the separating equilibria that lack robustness. See also Fagart (1996) for another specification of the game. She extends the work of Rothschild and Stiglitz (1976). Her paper presents a game where two principals compete for an agent, when the agent has private information. By considering a certain type of uncertainty, competition in markets with asymmetric information does not always imply a loss of efficiency.

⁴³This work is technically not introducing dynamics, but an insurer characteristic/constraint. It is discussed here to keep the literature roughly in chronological order.

show that in the standard insurance model, the WMS allocation is an equilibrium allocation, and furthermore that it is unique under a specific condition that rules out the use of on path latent contracts.

Whereas the above work explicitly models dynamics, another strand of the recent literature highlights insurer or contract features. Picard (2014) shows that the WMS allocation is an equilibrium allocating when contracts are participating. Participating contracts create externalities which render cream-skimming contracts unattractive. Mimra and Wambach (2019b) explicitly model the possibility of insurer insolvency, which creates a similar externality that allows to sustain the WMS allocation.⁴⁴ Dosis (2022) shows that a price cap can guarantee equilibrium existence under the assumption that each insurer has to have the full set of potential contracts on offer. Cream-skimming is not possible as the price cap prevents deviating insurers to drop bad risks by increasing the price on their contracts.

Our discussion has focused on game-theoretic approaches. In an influential recent work, Azevedo and Gottlieb (2017) propose a perfectly competitive model of markets with adverse selection that encompasses multiple dimensions of private information. The price-taking competitive equilibrium concept is that of a set of prices and an allocation such that all consumers optimize and prices equal the average cost of supplying each contract, and an additional requirement that can be interpreted as a free entry notion. By ruling out cross-subsidization, the equilibrium allocation is of the Rothschild-Stiglitz form (and thus potentially not second-best efficient), and coincides with it in the standard insurance market models. Levy and Veiga (2023) adopt the Azevedo and Gottlieb (2017) competitive equilibrium concept and analyze the effects of contract regulation (minimum and maximum coverage levels) on equilibrium and welfare.

Finally, as we will see in Section 7, another possibility to deal with equilibrium issues is to use risk categorization (see Dionne and Rothschild, 2014 and Crocker et al., 2024, for more detailed analyses).

4.3 Multiperiod contracts and competition

The aspect of competition raises new technical and economic issues on multiperiod contracting. Indeed, the value of information affects the process of decision-making in a competitive insurance market considerably. Let us begin with Cooper and Hayes' (1987) analysis of two-period contracts with full commitment on the supply side.

⁴⁴Picard (2014) and Mimra and Wambach (2019b) are discussed in more detail in section 7.4 on the role of mutual insurance, participating contracts and insurer insolvency.

4.3.1 Full commitment

Cooper and Hayes use the Nash equilibrium concept in a two-period game where the equilibrium must be separating.⁴⁵ They consider two different behaviors related to commitment on the demand side. First, both insurers and insureds commit themselves to the two-period contracts (without possibility of renegotiation) and second, the insurers commit to a two-period contract but the contract is not binding on insureds. We will refer these respective situations as contracts with *full commitment* and *with semi-commitment*, respectively. When competitive firms can bind agents to the two periods, it is easy to show that, in the separating solution, the contracts offered are qualitatively identical to that of the monopoly solution with commitment: high-risk agents receive full insurance at an actuarial price in each period while low-risk agents face price and quantity adjustments in the second period. Suppose that q_H is such that a Rothschild and Stiglitz equilibrium is second-best efficient. It can be shown that the two-period contract with full commitment dominates a repetition of Rothschild-Stiglitz contracts without memory. As for the monopoly case, this result is due to the memory effect (see Chiappori et al., 1994 for a survey on the memory effect).

When the authors relax the strong commitment assumption in favor of semi-commitment, and consider that insureds can costlessly switch to other firms in the second period, they show that the presence of second-period competition limits but does not destroy the use of experience rating as a sorting device. The difference between the results with full commitment and semi-commitment is explained by the fact that the punishment possibilities for period-one accidents are reduced by the presence of other firms that offer single-period contracts in the second period.

The semi-commitment result was obtained by assuming that, in the second period, entrant firms offer single-period contracts without any knowledge of insureds' accident histories or their choice of contract in the first period. The new firms' optimal behavior is to offer Rothschild-Stiglitz separating contracts⁴⁶ to the market.⁴⁷ By taking this decision as given, the design of the optimal two-period contract by competitive firms with semi-commitment has to take into account at least one supplementary binding constraint (no-switching constraint) that reduces social welfare compared to full commitment. The formal problem consists of maximizing the low-risks' two-period expected utility by choosing

⁴⁵In other words, they implicitly assume that the conditions to obtain a Nash separating equilibrium in a single-period contract are sufficient for an equilibrium to exist in their two-period model.

⁴⁶The Rothschild-Stiglitz contracts are not necessarily the best policy rival firms can offer. Assuming that outside options are fixed is restrictive. This issue is discussed in the next section.

⁴⁷The authors limited their focus to separating solutions.

C_H^2 and C_L^2 under the incentive compatibility constraints, the nonnegative intertemporal expected profit constraint and the *no-switching* constraints:

Problem 5

$$\begin{aligned} & \max_{C_H^2, C_L^2} V(C_L^2 | p_L) \\ & \text{s.t.} \\ & V(C_i^2 | p_i) \geq V(C_j^2 | p_i) \quad i, j = H, L, \quad i \neq j \\ & \pi(C_L | p_L) + [p_L \pi(C_{La} | p_L) + (1 - p_L) \pi(C_{Ln} | p_L)] \geq 0 \\ & V(C_{is} | p_i) \geq V(C_i^* | p_i) \quad i = H, L \quad s = a, n. \end{aligned}$$

By the constraint of non-negative expected profits earned on the low-risks' multiperiod contract, this model rules out the possibility of insurers' offering cross-subsidizations between the low and the high-risks (and circumvent any problems of inexistence of Nash equilibrium). Because this constraint is obviously binding at the optimum, Cooper and Hayes (1987) allow only intertemporal transfers.

Using the above model, Cooper and Hayes (1987) proved the following results, summarized by Proposition 11:

Proposition 11 *Under the assumption that a Nash equilibrium exists, the optimal two-period contract with semi-commitment is characterized by the following properties:*

1) *High-risk individuals obtain full insurance coverage and are not experience rated: $V(C_{Ha}^* | p_H) = V(C_{Hn}^* | p_H) = V(C_H^* | p_H) = U(W - \alpha_H^*)$;*

while low-risk individuals receive only partial insurance coverage and are experience rated: $V(C_{La}^ | p_L) < V(C_{Ln}^* | p_L)$;*

2) *High-risk agents are indifferent between their contract and that intended for low-risks, while low-risks strictly prefer their contract:*

$$V(C_H^{2*} | p_H) = V(C_L^{2*} | p_H) \text{ and } V(C_L^{2*} | p_L) > V(C_H^{2*} | p_L);$$

3) *Both high and low-risks obtain a consumer surplus:*

$$V(C_i^{2*} | p_i) > 2V(C^0 | p_i), \quad i = H, L;$$

4) *The pattern of temporal profits is highballing on low-risks' contracts and flat on high-risks' ones:*

$$\begin{aligned} & \pi(C_L^* | p_L) \geq 0 \geq [p_L \pi(C_{La}^* | p_L) + (1 - p_L) \pi(C_{Ln}^* | p_L)] \\ & \text{and } \pi(C_H^* | p_H) = \pi(C_{Ha}^* | p_H) = \pi(C_{Hn}^* | p_H) = 0. \end{aligned}$$

In other words, the presence of competition, combined with the agents' inability to enforce binding multiperiod contracts, reduces the usefulness of long term contracts as a sorting device and consequently, the potential gains of long term relationships. This conclusion is similar to that obtained in the monopoly case (in which the principal cannot commit on nonrenegotiation) because the

no-switching constraints imposed by competition can be reinterpreted as rationality constraints in a monopolistic situation.

The fourth property in Proposition 11 means that, at equilibrium, firms make positive expected profits on old low-risk insureds (by earning positive profits on the low-risks' first period contract) and expected losses on new low-risk insureds (by making losses on the second-period contract of low-risks who suffered a first-period loss, greater than positive profits on the low-risks' contract corresponding to the no-loss state in the first period). In aggregate, expected two-period profits from low-risks are zero.

As in the monopoly situation, all the consumers self-select in the first period and only low-risk insureds are offered an experience-rated contract in the second period based on their accident history.⁴⁸ This arrangement provides an appropriate bonus for accident-free experience and ensures that low-risks who suffer an accident remain with the firm.⁴⁹ This temporal profit pattern, also called *highballing* by D'Arcy and Doherty (1990), was shown to contrast with the *lowballing* predicted in dynamic models without commitment. In particular, D'Arcy and Doherty compare the results obtained by Cooper and Hayes (1987) under the full commitment assumption with those of the *lowballing* predicted by Kunreuther and Pauly (1985) in a price competition. With similar assumptions on commitment, Nilssen (2000) also obtains a *lowballing* prediction in the classic situation of competition in price-quantity contracts.

Although Cooper and Hayes (1987) were the first to consider a repeated insurance problem with adverse selection and full commitment, some assumptions are not realistic, namely the insurers' ability to commit to long term relationships. Indeed, because the first-period contract choices do reveal the individual risks, the initial agreement on the second-period contract could be renegotiated at the beginning of the second period (under full information) in a way that would improve the welfare of both parties. Consequently, the two-period contract with full commitment is Pareto-inefficient *ex post*, i.e. relative to the information acquired by insurers at that time. Other articles in the literature have investigated other concepts of relationships between an insurer and its insureds, involving limited commitment: the *no-commitment* assumption represents the polar case of the full commitment situation (section 4.3.2) and the *commitment with renegotiation* appears to be an intermediate case between full commitment and no-commitment (section 4.3.3).

As a result of the strong hypotheses above, the literature obtains the same predictions as in the static model about the equilibrium existence issue⁵⁰ and

⁴⁸But not on their contract choice.

⁴⁹The corresponding expected utility of the low-risk individual who did not have an accident in the first period is strictly greater at equilibrium than that corresponding to the entrant one-period contract.

⁵⁰Cross-subsidizations between risk types remain inconsistent with equilibrium, such that problems for equilibrium existence also exist in a multiperiod context.

about the self-selection principle. These predictions do not hold any longer when we assume limited commitment and/or endogenous outside options.

4.3.2 No-commitment

In this section, the attention is paid to competitive insurance models in which the contractual parties can commit only to one-period incentive schemes, i.e. where insurers can write short-term contracts, but not long-term contracts. The no-commitment is bilateral in the sense that each insured can switch to another company in period two if he decides to do so. Such situations are particularly relevant in liability insurance (automobile or health insurance for example) where long-term contracts are rarely signed. Despite this inability to commit, both parties can sign a first-period contract that should be followed by second-period contracts that are conditionally optimal and experience-rated. This sequence of one-period contracts gives rise to a level of intertemporal welfare lower than that of full commitment, but, in some cases, higher than in a repetition of static contracts without memory.

Kunreuther and Pauly (1985) were the first to study a multiperiod model without commitment in a competitive insurance context. However, their investigation is not really an extension of the Rothschild and Stiglitz' analysis because the authors consider competition in price and not in price-quantity.⁵¹ They argue that insurers are unable to write exclusive contracts; instead they propose that insurers offer pure price contracts only (Pauly, 1974). They also assume that consumers are myopic: they choose the firm that makes the most attractive offer in the current period. At the other extreme, the classic dynamic literature supposes that individuals have perfect foresight in the sense that they maximize the discounted expected utility over the planning horizon.

Despite the major difference in the assumption about the way insurers compete, their model leads to the same lowballing prediction as other studies, like the one developed by Nilssen (2000), using the basic framework of the Rothschild and Stiglitz (1976) model where firms compete by offering price-quantity contracts. Insurers make expected losses in the first period and earn expected profits on the policies they renew. This prediction of lock-in is due to the assumption that insurers do not write long-term contracts while, as we saw, Cooper and Hayes (1987) permitted long-term contracting. In Nilssen's (2000) model, an important result is to show that pooling contracts could emerge in dynamic equilibrium (pooling on the new insureds) when the ability to commit lacks in the relationships, which makes the cross-subsidizations compatible with equilibrium. Contrary to the Kunreuther and Pauly (1985) model, the absence of commitment does not rule out separation.

⁵¹They let insurers offer contracts specifying a per-unit premium for a given amount of coverage.

The program presented below (Problem 6) includes Nilssen's (2000) model as a particular case (more precisely, for both $x_H = 1, x_L = 0$ where $x_i \in [0; 1]$ measures the level of separation of type i). In other words, we introduce strategies played by insureds in Nilssen's (2000) model, such that at equilibrium, semi-pooling can emerge in the first period, followed by separation in the second period. This technical process, also labeled *randomization*, serves to defer the revelation of information and thus encourages compliance with sequential optimality constraints required by models with limited commitment. It was used by Hosios and Peters (1989), as we saw, in a monopoly situation without commitment and by Dionne and Doherty (1994) in a competitive context with commitment and renegotiation.⁵²

Solving the two-period model without commitment requires the use of the concept of Nash Perfect Bayesian Equilibrium (NPBE).⁵³ Given this notion of sequential equilibrium, we work backwards and begin by providing a description of the Nash equilibrium in the last period.

In period 2, \widehat{C}_{ia} and \widehat{C}_{in} solve the following subprograms imposed by the constraints of sequential optimality, for $s \in \{a, n\}$ respectively where a means accident in the first period and n means no-accident:

Problem 6

$$\begin{aligned} \widehat{C}_{is} \in \arg \max \quad & \sum_{i=H,L} q_{is}(x_i)\pi(C_{is} | p_i) \\ & s.t. \\ V(C_{is} | p_i) \geq & V(C_{js} | p_i) \quad i, j = H, L, \quad i \neq j \\ V(C_{is} | p_i) \geq & V(C_i^{RS} | p_i) \quad i = H, L \end{aligned}$$

where posterior beliefs⁵⁴ are defined by

$$\begin{aligned} q_{ia}(x_i) &= \frac{q_i p_i x_i}{\sum_{k=H,L} q_k p_k x_k} \\ \text{and } q_{in}(x_i) &= \frac{q_i(1-p_i)x_i}{\sum_{k=H,L} q_k(1-p_k)x_k}, \quad i = H, L. \end{aligned}$$

For given beliefs, the second-period optimization subprogram is similar, in some sense, to a single-period monopoly insurance model with adverse selection

⁵²On limited commitment and randomized strategies, see also Dionne and Fluet (2000).

⁵³This concept implies that the set of strategies satisfies sequential rationality given the system of beliefs, and that the system of beliefs is obtained from both strategies and observed actions using Bayes' rule whenever possible.

⁵⁴Put differently, $q_{ia}(x_i)$ and $q_{in}(x_i)$ are the probabilities at the beginning of the second period that, among the insureds having chosen the pooling contract in the first period, an insured belongs to the i -risk class if he has suffered a loss or no loss in the first period respectively.

(Stiglitz 1977, in section 3.2) for a subgroup of insureds and where no-switching constraints correspond to usual participation constraints. In the absence of commitment and because of informational asymmetries between insurers, each informed firm can use its knowledge of its old insureds to earn positive profits in the second period. However, this profit is limited by the possibility that old insureds switch to another company at the beginning of the second period. Contrary to a rival company, a firm that proposes sets of contracts in the second period to its insureds can distinguish among accident-groups on the basis of past accident observations. Each company acquires over time an informational advantage relative to the rest of competing firms on the insurance market.

The PBE of the complete game is a sequence of one-period contracts $(C_i^*, C_{ia}^*, C_{in}^*)$ for every $i = H, L$, such that:

Problem 7

$$(C_i^*, C_{ia}^*, C_{in}^*) \in \arg \max_{(C_i, C_{ia}, C_{in})} V(C_L | p_L) + \delta[p_L V(\widehat{C_{La}} | p_L) + (1-p_L)V(\widehat{C_{Ln}} | p_L)]$$

s.t.

$$x_i(1 + \delta)V(C_i^{RS} | p_i) + (1 - x_i)[V(C_i | p_i) + \delta(p_i V(\widehat{C_{ia}} | p_i) + (1 - p_i)V(\widehat{C_{in}} | p_i))] \\ \geq V(C_j | p_i) + \delta(p_i V(\widehat{C_{ja}} | p_i) + (1 - p_i)V(\widehat{C_{jn}} | p_i))$$

$$\sum_{i=H,L} q_i(x_i)\pi(C_i | p_i) + \delta \left[\sum_{i=H,L} q_{ia}(x_i)\pi(\widehat{C_{ia}} | p_i) + \sum_{i=H,L} q_{in}(x_i)\pi(\widehat{C_{in}} | p_i) \right] \geq 0$$

where $\widehat{C_{La}}, \widehat{C_{Ln}}$ solve Problem 6 for $s = a, n$ respectively.

Problem 7 provides the predictions summarized in Proposition 12.

Proposition 12 *In the presence of private information, each company may increase the individuals welfare by offering two contracts, a sequence of one-period contracts and a multiperiod contract without commitment with the following characteristics:*

1) *Both high and low-risk classes obtain partial insurance coverage in each period and are experience rated: $V(C_{ia}^* | p_i) \leq V(C_{in}^* | p_i)$, $i = H, L$;*

2) *High-risk classes are indifferent between a mix of a sequence of Rothschild-Stiglitz contracts and the multiperiod contract, also subscribed by low-risk individuals:*

$$x_H(1 + \delta)V(C_H^{RS} | p_H) + (1 - x_H)V(C_H^{2*} | p_H) = V(C_L^{2*} | p_H)$$

and the low-risks strictly prefer the multiperiod contract:

$$V(C_L^{2*} | p_L) > x_L(1 + \delta)V(C_L^{RS} | p_L) + (1 - x_L)V(C_L^{2*} | p_L), \quad x_L \in [0, 1];$$

3) *High and low-risk individuals obtain a consumer surplus:*

$$V(C_i^{2*} | p_i) > (1 + \delta)V(C^0 | p_i), \quad i = H, L;$$

4) *Aggregate expected profits earned on the multiperiod contract increase over time:* $\sum_{i=H,L} q_i(x_i)\pi(C_i^* | p_i) < \sum_{i=H,L} \sum_{s=a,n} q_{is}(x_i)\pi(C_{is}^* | p_i)$.

Concerning the existence property, it can be shown that a Nash Perfect Bayesian Equilibrium exists for some values of parameters (i.e. for every q_H such that $q_H \geq q_H^{NC} (> q_H^{RS})$ where NC is for no commitment). As a consequence, the existence property of equilibrium is guaranteed for a set of parameters smaller than in the static model. More importantly, this model exhibits a lowballing configuration of intertemporal profits (increasing profits over time; each firm earns a positive expected profit on its old customers because it controls information on past experience), contrary to the highballing prediction resulting from models with full commitment.

Finally, particular attention could be paid to interfirm communication and the model could make the outside options endogenous to the information revealed over time. In Cooper and Hayes' (1987) and Nilssen's (2000) models and in most dynamic models, firms are supposed to offer the same contract to a new customer (the outside option is C_i^{RS}), whatever his contractual path and his accident history. In other words, it is implicitly assumed that the information revealed by the accident records and by contractual choices does not become public.⁵⁵ However, this assumption is not very realistic with regard to the presence, in some countries, of a specific regulatory law that obliges insurers to make these data public.⁵⁶ This is the case in France and in most European countries for automobile insurance, where the free availability of accident records is a statutory situation. Consequently, models with endogenous outside options would be more appropriate to describe the functioning of the competitive insurance market in these countries. To evaluate the effects of a regulatory law about interfirm communication, let us consider the extreme situation in which insurers are constrained to make data records public, such that rival firms do have free access to all accident records. Formally, this amounts to replacing C_i^{RS} by C_i^{cc} in no-switching constraints of Problem 6 (C_i^{cc} is the best contract a rival uninformed company can offer to i-risk type at the beginning of period 2).

In other words, C_i^{cc} describes the switching opportunities of any insured i and depends on x_i . At one extreme case, when the first-period contracts are fully separating, the contract choice reveals individual risk-types to any insurer on the insurance market, and C_i^{cc} will be the first-best contract C_i^{FB} . If competing firms have identical knowledge about insureds risks over time, no experience rating is sustainable in equilibrium and allocative inefficiency results from dynamic contractual relationships. The "too large" amount of revealed information destroys efficiency and eliminates dynamic equilibria. In

⁵⁵When an individual quits a company A and begins a new relationship with a company B, he is considered by the latter as a new customer on the insurance market.

⁵⁶For a more detailed argumentation of information sharing, see Kunreuther and Pauly (1985), D'Arcy and Doherty (1990), and Dionne (2001).

contrast, when rival firms do not have access to accident records, equilibrium involves experience-rating and dynamic contracts achieve second-best optimality, because informational asymmetries between competing firms make cross-subsidization compatible with the Nash equilibrium. As a consequence, insureds are always better off when accidents remain private information.

See also Section 7.3 for a discussion of recent works, both empirical and theoretical, that address this problem of information asymmetric between the incumbent insurer and its competitors when there is no adverse selection in period 1. In a context of symmetric imperfect information, De Garidel-Thoron (2005) also finds that accident claims should not be shared by insurers.

The next section is devoted to an analysis of multiperiod contracts under an intermediary level of commitment from insurers.

4.4 Commitment and renegotiation

Dionne and Doherty (1994) introduced the concept of renegotiation in long-term relationships in insurance markets. Here, the two-period contracts are considered where insureds can leave the relation at the end of the first period and the insurer is bound by a multiperiod agreement. It differs from Cooper and Hayes' (1987) model due to the possibility of renegotiation. Indeed, insurers are allowed to make a proposition of contract renegotiation with their insureds which can be accepted or rejected. In other words, parties cannot precommit to not make Pareto-improving changes based on information revealed at the end of the first period. As shown in Dionne and Doherty (1994), the Cooper and Hayes' (1987) solution is not renegotiation-proof. This means that sequential optimality fails because parties' objectives change over time. If renegotiation cannot be ruled out, the company and its insureds anticipate it, and this will change the nature of the contracts. Thus, to ensure robustness against renegotiation procedure described above, we must impose either the constraint of pooling in the first period or the constraint of full insurance for both types in the second period in addition to standard constraints in Cooper and Hayes' (1987) optimization program. The new program can be written as Problem 7 except for the second-period constraints imposed by sequential optimality. Indeed, renegotiation-proofness means that the second-period contracts are robust to Pareto-improving changes and not only for increasing the insurers' welfare. Consequently, second-period contracts cannot be solved as a subprogram that maximizes insurers' expected profits. In contrast, they must solve, in the last period, a standard competitive program that optimizes the low-risks welfare (in each group a and n). Moreover, no-switching constraints must appear in these subprograms in a similar way as in the model without commitment.

If we consider a general model in which all kinds of transfers are allowed (intertemporal and intertype transfers), problem 6 can be rewritten in the context of semi-commitment with renegotiation as follows:

Problem 8

$$\begin{aligned} \widehat{C}_{is} &\in \arg \max V(C_{Ls} | p_L) \text{ for } s = a, n \\ &\text{s.t.} \\ V(C_{is} | p_i) &\geq V(C_{js} | p_i) \quad i, j = H, L, \quad i \neq j \\ \sum_{i=H,L} q_{is}(x_i)\pi(C_{is} | p_i) &\geq \bar{\pi}_s \\ V(C_{is} | p_i) &\geq V(C_i^{RS} | p_i) \quad i = H, L. \end{aligned}$$

Dionne and Doherty (1994) first show that fully separating strategies, once made robust to renegotiation, degenerate to an outcome that amounts to that of a replication of single-period contracts in terms of welfare, when insureds are bound in relationships. If insureds are allowed to leave their company at the end of period 1, the program includes, in addition, no-switching constraints. As a result of this more constrained problem, the outcome will be worse in terms of welfare relative to a sequence of static contracts without memory. This negative result on separating contracts suggests efficiency will be attained by a partial revelation of information over time (as in the no-commitment model). Dionne and Doherty (1994) then show that the solution may involve semi-pooling in the first period followed by separated contracts. They argue that the equilibrium is fully separating when the discount factor is low and tends to a pooling for large discount factors. They also obtain a highballing configuration of intertemporal profits, contrary to the lowballing prediction resulting from models without commitment. Thus, commitment with renegotiation provides the same predictions as those in Proposition 12 except for the fourth result, which becomes:

$$\sum_{i=H,L} q_i(x_i)\pi(C_i^* | p_i) > \sum_{i=H,L} \sum_{s=a,n} q_{is}(x_i)\pi(C_{is}^* | p_i).$$

However, if a more general model is considered, in which outside options are endogenous (in which case C_i^{cc} replace C_i^{RS} in Problem 8, $i=H,L$), the configuration in equilibrium does not necessarily exhibit a decreasing profile of intertemporal profits for the company, meaning that models with commitment and renegotiation do not necessarily rule out the possibility of lock-in.⁵⁷ As in models without commitment, insureds are always better off when the information about accident records remains private, i.e. in a statutory situation where no regulatory law requires companies to make record data public.

⁵⁷However, it is possible to establish that a competitive insurance market always has an equilibrium, due to the compatibility of cross-subsidization with equilibrium, as opposed to the result in static models. The economic intuition is the following: an additional instrument can serve to make rival offers less attractive. It consists in informed insurers' offering unprofitable contracts in the second period. This instrument is possibly used in a case of commitment with renegotiation but cannot be enforced in no-commitment situations.

Finally, the issue of consumer lock-in and the pattern of temporal profits should motivate researchers to undertake empirical investigations of the significance of adverse selection and of the testable predictions that permit discrimination between the competing models. To our knowledge, only a few published studies have investigated these questions with multi-period data; their conclusions can go in opposite directions. D’Arcy and Doherty (1990) found evidence of lowballing that supports the non-commitment assumption while Dionne and Doherty (1994) report that a significant group of insurers in California used highballing – a result that is more in line with some form of commitment. It is interesting to observe that this group of insurers attracts selective portfolios with disproportionate numbers of low-risks. This result reinforces the idea that some form of commitment introduces more efficiency and the fact that there is adverse selection in this market.

In an environment where types evolve over time (the probability distributions follow a Markov process), Farinha Luz (2022) study a multiperiod model in a competitive insurance context with full commitment. Here again, the policyholders make a choice between a full coverage priced at a premium fixed in perpetuity and partial insurance followed by offers contingent on the occurrence of future accidents. Surprisingly, the intertemporal pricing scheme is back-loaded, although policy options within the optimal menu become more attractive over time. Farinha Luz (2022) has focused on pure strategies but he conjectures that a similar mixed strategy equilibrium may exist in the studied setting such that the equilibrium would involve randomization over mechanisms (with regard to what is done in Farinha Luz, 2017).

Furthermore, in a context of risk evolving over time, state regulations often prohibit companies from using accident or loss histories in their pricing scheme (in particular life insurance and health insurance), in order to protect consumers against premium reclassification risk. Long term contracts may permit addressing reclassification risk without inducing adverse selection. On the contrary, the lack of commitment compromises the insurance against reclassification risk and creates an adverse selection. There is now a new literature on dynamic health insurance contracting, mainly focusing on reclassification risk, with an emphasis on state regulations (see Handel et al. 2015 and Ghili et al. 2021 for a quantitative analysis of welfare costs of adverse selection in health insurance under different hypotheses of regulations, and Hendel 2017 for an overview of the impact of these regulations on dynamic selection and reclassification risk).

5 Moral hazard and adverse selection

Although in many situations principals face adverse selection and moral hazard problems simultaneously when they design contracts, these two types of asymmetric information have been given separate treatments so far in the economic

literature on risk-sharing agreements. Both information problems have been integrated into a single model where all the parties of the contract are risk neutral (Laffont and Tirole, 1986; Picard, 1987; Caillaud *et al*, 1988; Guesnerie *et al*, 1988). Although these models involve uncertainty, they are unable to explain arrangements where at least one party is risk averse. In particular they do not apply to insurance. More recently, some authors have attempted to integrate both information problems into a single model where the agent is risk averse.

As discussed by Dionne and Lasserre (1988) such an integration of both information problems is warranted on empirical grounds. Applied studies are still few in this area, but researchers will find it difficult to avoid considering both kinds of information asymmetry (see, however, Dionne *et al.*, 2013b).

5.1 Monopoly and multi-period contracts

Dionne and Lasserre (1988) show how it is possible to achieve a second-best allocation of risks when moral hazard and adverse selection problems exist simultaneously. While they draw heavily on the contributions of Rubinstein and Yaari (1983), Dionne (1983) and Dionne and Lasserre (1985), the integration of the two types of information problems is not a straightforward exercise. Given that an agent who has made a false announcement may now choose an action that is statistically compatible with his announcement, false announcements may go undetected. They propose a contract under which the agent cannot profit from this additional degree of freedom. Under a combination of moral hazard and adverse selection, several types of customers can adopt different care levels such that they have identical expected losses. When this happens, it is impossible to distinguish those who produce an efficient level of care from the others on the basis of average losses.

However, deviant behaviors can be detected by monitoring deviations from the mean. Thus the insurer's strategy can be written with more than one simple aggregate (as in Dionne and Lasserre, 1985, and Rubinstein and Yaari, 1983). In Dionne and Lasserre (1988) the principal has to monitor two aggregates, the average loss experienced by a given agent and its squared deviation from the mean. It was sufficient to get the desired result because in their model the information problem has only two dimensions. More generally, the insurer would have to monitor one moment of the distribution for each hidden dimension.

Combining moral hazard with adverse selection problems in models that use past experience might involve some synergetic effects. In the model presented in Dionne and Lasserre (1988), the same information required to eliminate either the moral hazard problem alone (Rubinstein and Yaari, 1983) or adverse selection alone (Dionne and Lasserre, 1988) is used to remove both problems

simultaneously. A related subject concerns the efficient use of past information, and the allocation of instruments, toward the solution of each particular information problem. Self-selection mechanisms have long been proposed in response to adverse selection while nonlinear pricing was put forth as a solution to moral hazard. In one-period contracts both procedures used separately involve inefficiency (partial insurance) which can be reduced by the introduction of time in the contracts. Dionne and Lasserre (1988) show that self-selection may help solve both moral hazard problems and adverse selection problems. We will now discuss how the use of two instruments may improve resource allocation and welfare when both problems are present simultaneously in single-period competitive contracts.

In a static model which can be considered as a special case of the Dionne and Lasserre's (1988) model, Chassagnon (1994) studies the optimality of a one-period model when both problems are present simultaneously. Three results are of interest in this paper: 1) the Spence-Mirlees property is not always verified. Indifference curves may have more than one intersection point; 2) contrarily to the Stiglitz (1977) model where the low-risk individual may not have access to any insurance coverage, in Chassagnon's (1994) model, there are configurations (in particular, the configuration *du pas de danse*, 'dance step') where all agents obtain insurance; finally, 3) both types of agents may receive a positive rent according to their relative number in the economy.

The model is specific in the sense that the accident probabilities keep the same order when the effort level is the same. Suppose that there are only two levels of efforts that characterize the accident probabilities of type i : $\underline{p}_i < \bar{p}_i$, $i = H, L$. In Chassagnon's model, $\underline{p}_H > \underline{p}_L$ and $\bar{p}_H > \bar{p}_L$ while \underline{p}_H can be lower than \bar{p}_L . In fact the effect of introducing moral hazard in the pure principal-agent model becomes interesting when the high-risk individual is more efficient at care activities than the low-risk individual. Otherwise, when $\underline{p}_H > \bar{p}_L$, the results are the same as in the pure adverse selection selection model where only the H type receives a positive rent.

5.2 Competitive contracts

One of the arguments often used to justify the prohibition of risk categorization is that it is based on fixed or exogenous characteristics such as age, race and sex. However, as pointed out by Bond and Crocker (1991), insurers also use other characteristics that are chosen by individuals. They extend Crocker and Snow (1986) previous analysis of risk categorization in the presence of adverse selection and examine the equilibrium and efficiency implications of risk categorization based on consumption goods that are statistically related to individual's risks, which they termed "correlative products."

Formally, their model introduces endogenous categorization in an environment characterized by both moral hazard and adverse selection. They show that while there is a natural tension between the sorting of risk classes engendered by adverse selection and the correction of externalities induced by moral hazard, the use of risk classification improves efficiency in resource allocation. They also obtain that the sorting of risks based on correlative consumption may give a first-best allocation as Nash equilibria when adverse selection is not too severe, and when the insurer can observe individual consumption of the hazardous good.

This is particularly interesting as an alternative view of how firms, in practice, may overcome the nonexistence of Nash equilibrium problems. They then consider the case where the insurer cannot observe both the individual's consumption and the individual's characteristics. However, the planner can observe aggregate production of the good. They show that taxation of the consumption good now has two roles (reducing moral hazard and relaxing self-selection constraints) that permit Pareto improvements.

Chassagnon and Chiappori (1995) also propose an extension to the pure adverse selection model to consider incentives or moral hazard: the individual's probability of accidents is no longer completely exogenous; it depends on the agent's level of effort. In general, different agents choose different effort levels even when facing the same insurance contract. The equilibrium effort level does not depend on the level of accident probability but on its derivative. Consequently, the H type may have more incentive to produce safety to have access to a low insurance premium but he may not have access to efficient technology.

As in Chassagnon (1994), indifference curves may intersect more than once which rules out the Spence-Mirrlees condition. As a result, when an equilibrium exists, it may correspond to many Rothschild and Stiglitz equilibria, a situation that is ruled out in the pure adverse selection model. Consequently, the equilibrium must be ranked, and Chassagnon and Chiappori (1995) use Hahn's concept of equilibrium to select the Pareto efficient equilibrium from the Rothschild-Stiglitz candidates. In the pure adverse selection world, both equilibrium concepts are equivalent.

In the same spirit, De Meza and Webb (2001) formalize the argument of "advantageous selection" and examine the relation between risk preference and choice of precaution with a specification that the taste-for-risk parameter is additive in wealth. Under this non-monetary formulation of the cost of prevention, the authors show that the single-crossing condition between risk-neutral and risk-averse individuals may not be satisfied (while Jullien et al. (2007) show that this property always holds with a monetary formulation of the cost of precaution).

As a starting point, cautious types (more inclined to buy insurance and to put forth more effort) initially coexist with risk-tolerant types (disinclined

to insure and to take precautions). The precautionary effort is thus positively correlated with insurance purchase. Depending on parameter values, separating, full pooling and partial pooling equilibria are possible. What allows pooling (partial or full) is the double crossing of indifference curves.

Another important conclusion is about the condition to obtain an equilibrium. It was shown in a previous section that a Rothschild-Stiglitz equilibrium exists if and only if there are enough high-risk agents in the economy. When both problems are present simultaneously, this condition is no longer true. Depending on the parameters of the model, an equilibrium may exist whatever the proportions of agents of different types; or may even fail to exist whatever the respective proportions.

Finally, it is important to emphasize that the individual with higher accident probability, at equilibrium, always has access to the more comprehensive insurance coverage, a conclusion that is shared by the standard model. However, here, this individual is not necessarily of type H . This result is important for empirical research on the presence of asymmetric information problems.⁵⁸

In contrast, several studies suggest that the correlation between risk level and insurance purchases is ambiguous. The above-mentioned "advantageous selection" is called "propitious selection" by De Donder and Hindriks (2009), who also assume that applicants who are highly risk averse are more likely to try to reduce the hazard and to purchase insurance. In a model with two types of individuals differing in risk aversion, two properties (regularity and single-crossing) formalize the propitious argument. Under these two properties, the more risk-averse individuals will both exert more precaution and have a higher willingness to pay for insurance. De Donder and Hindriks (2009) thus prove that there cannot exist a pooling equilibrium. Indeed, a deviating firm can always propose a profitable contract, attractive only for the more risk-averse agents (who are also less risky in accordance with the propitious argument). Finally, the equilibrium contracts are separating with the more risk-averse individuals buying more insurance. Despite the propitious selection, the correlation between risk levels and insurance purchases is ambiguous at equilibrium: even though more risk averse agents behave more cautiously, they also buy more insurance at equilibrium, and with moral hazard, risk increases with coverage.

In a two-period model combining moral hazard and adverse selection, Sonnenholzner and Wambach (2009) propose another explanation of why the relationship between level of risk and insurance coverage can be of any sign. They stress the role of (unobservable) individual personal discount in explaining the

⁵⁸See Cohen and Siegelman (2010) for a survey and a discussion about empirical work on the coverage-risk correlation that the pure asymmetric information model predicts. See also Chiappori and Salanié (2013) for a more recent review of empirical models on asymmetric information and Dionne et al. (2013b) for a model that separates moral hazard from adverse selection and learning.

decision to purchase insurance. Impatient individuals (with a high discount factor) initially coexist with patient individuals (with a low discount factor). A separating equilibrium exists in which patient consumers exert high precaution and are partially covered with a profit-making insurance contract, while the impatient consumers exert low effort and buy a contract with lower coverage or even prefer to remain uninsured. In contrast with the usual prediction, there is a negative correlation between risk and quantity.^{59 60}

These works are very close to the literature on multi-dimensional adverse selection where preferences are not necessarily single-crossing (See section 7.2 in this Chapter). However in these multi-dimensional models, the higher risks buy more insurance.

6 Adverse selection when people can choose their risk status

An interesting twist on the adverse selection problem is to allow individuals' information status to vary along with their risk status. A traditional adverse selection problem arises when individuals know their risk status but the insurer does not. What happens in a market where some insureds know their risk status and others do not? The answer to this question depends on whether the information status is observed by the insurer. A further variation arises when the uninformed insureds can take a test to ascertain their risk status. Whether they choose to take the test depends on the menu they will be offered when they become informed and how the utility of this menu compares with the utility of remaining uninformed. Thus, the adverse selection problem becomes entwined with the value of information.

⁵⁹Without loss of generality, Fombaron and Milcent (2007) obtain the same conclusion in a model of health insurance in which they introduce a gap between the reservation utilities. This formulation implies that the low-risks may be more inclined to buy insurance than the high-risks when loss probabilities are symmetric information. This finding suggests that preference heterogeneity may be sufficient in explaining the opposite selection of insurance coverage in various markets.

⁶⁰Cutler et al. (2008) present empirical evidence in life insurance and in long-term care insurance in the US that is consistent with this negative correlation (those who have more insurance are a lower risk because they produce more prevention).

However, in the long-term care insurance market in the United States, Finkelstein and McGarry (2006) find no statistically significant evidence of a coverage-risk correlation, while Browne (2006) suggests that high-risks purchase more insurance. In private health insurance in Germany and in a highly regulated market where insurers must offer long-term contracts with a one-sided commitment, Hofmann and Browne (2013) provide evidence suggesting that low-risk types are more likely to drop their coverage than high-risk types. The same evidence is supported by Finkelstein et al. (2005) in the long-term care insurance market in the United States. Moreover, in annuity markets for example, higher-risk people seem to have more insurance, as the standard theory would predict. See also Fang et al. (2008).

These questions are especially important in the health care debate. Progress in mapping the human genome is leading to more diagnostic tests and treatments for genetic disorders. It is important to know whether the equilibrium contract menus offered to informed insureds or employees are sufficiently attractive to encourage testing. The policy debate is extended by considering laws that govern the access of outsiders (such as employers and insurers) to medical records. For example, many laws require that medical records not be released to outsiders without the consent of the patient.⁶¹

6.1 A full information equilibrium with uninformed agents

The basic analysis will follow Doherty and Thistle (1996a). This model uses fairly standard adverse selection technology and is illustrated with health insurance. However, further works by Hoy and Polborn (2000) and Polborn et al. (2006) have shown that similar results can be derived in a life insurance market where there is no natural choice of coverage and where individuals can buy from multiple insurers.⁶²

Consider the simplest case in which there are initially three groups: uninformed, informed high-risks, and informed low-risks, which are labeled “ U ”, “ H ”, and “ L ” respectively. The contracts offered to each group will be labeled C_U , C_H , and C_L . We assume that type U has a probability q_H of being high-risk so we can rank the *a priori* loss probabilities as $p_H > p_U > p_L$. If insurers know the information and risk status of any individual (i.e., they know whether she is U , H or L) the equilibrium competitive contracts are the first best contracts C_U^* , C_H^* , and C_L^* depicted in Figure 6. This conclusion seems pretty obvious, but there is a potential problem to be cleared up before we can be comfortable with this equilibrium contract set. If all the uninformed chose

⁶¹For an overview of regulations and policy statements, see Hoel and Iversen (2002) and Viswanathan et al. (2007). The latter describe four major regulatory schemes for genetic information in several states, from no regulation to the most strict regulatory structure: in the Laissez-Faire approach, insurers have full freedom to request new tests or the disclosure of existing tests and to use test results in underwriting and rating; under the Disclosure Duty approach, individuals have to disclose to insurers the result of existing tests but cannot be required to undergo additional tests; while under the Consent Law approach, consumers are not required to divulge genetic test results but if they do, insurers may use this information. Finally, in the Strict Prohibition approach (there is a tendency in most countries to adopt this regulation of information in health insurance policies), insurers cannot request genetic tests and cannot use any genetic information in underwriting and rating. For a recent study on genetic testing in life insurance see Born (2019).

⁶²Because insurance companies don’t share information about the amount of insurance purchased by their customers in the context of life insurance, price-quantity contracts are not feasible. As a result, insurers can only quote a uniform (average) premium for all life insurance contracts. However, contrary to standard insurance setting, consumers can choose the size of loss, and this loss is positively dependent on the probability of death. Hence, increasing symmetric information about risk type leads to changes in the demand for life insurance and in the average price quoted by insurers, contrary to the standard setting.

to become informed, then the equilibrium contract set would contain only C_H^* and C_L^* . Thus, we must check when the uninformed would choose to become informed and face a lottery over C_H^* and C_L^* (the former if the test showed them to be high-risk and the latter if low-risk). In fact, the decision to become informed and receive policy C_H^* with probability q_H , and receive policy C_L^* with probability q_L , is a fair lottery (with the same expected value as staying with C_U^*) and would not be chosen by a risk-averse person. This confirms that the full information equilibrium is C_U^* , C_H^* , and C_L^* .

6.2 Sequential equilibrium with insurer observing information status but not risk type

It is a short step from this to consider what happens when the information status is known to the insurer but not the risk status of those who are informed.⁶³ For this case and the remaining ones in this section, we will look for sequential Nash equilibria. In this case, the insurer can offer a full information zero profit contract C_U^* to the uninformed and the standard Rothschild-Stiglitz contracts, C_H^* and C_L^* , as shown again in Figure 6. The intuition for this pair is clear when one considers that the uninformed can be identified and, by assumption, the informed high-risks cannot masquerade as uninformed. To confirm this in the equilibrium contract set, we must be sure that the uninformed choose to remain so. The previous paragraph explained that the uninformed would prefer to remain with C_U^* than take the fair lottery of C_H^* and C_L^* . C_L^* would be strictly preferred by an informed low-risk than the Rothschild-Stiglitz policy C_L^{**} (which has to satisfy the high-risk self-selection constraint). Thus, by transitivity, the uninformed would prefer to remain with C_U^* than face the lottery of C_H^* and C_L^{**} .

6.3 Sequential equilibrium when insurer cannot observe information status or risk type

We now come to the more interesting case in which the information status of individuals cannot be observed. This raises the possibility that people can take a test to become informed and, if the news is bad, pretend they are uninformed. Because the insurer cannot observe the information status, it has no way of separating these wolves in sheeps' clothing from the uninformed sheep. This presents a problem for the uninformed. To signal that they are really uninformed, and thus avoid subsidizing the high-risks, they must accept a contract that would satisfy a high-risk self-selection constraint. This contract, C_U'' , is

⁶³This case may stretch plausibility slightly because it is difficult to imagine an insurer being able to verify that someone claiming to be uninformed is not really an informed high-risk. However, we will present the case for completeness.

shown in Figure 6. Suppose for the time being that they accept this contract. Now what zero profit contract can be offered to the informed low-risks? To prevent the uninformed from buying a low-risk contract, the uninformed must satisfy an uninformed risk self-selection constraint and such a contract set is C''_L . Can this triplet, C^*_H , C''_U , C''_L be an equilibrium? The answer depends on the costs of information.

If the uninformed could choose to stay at C''_U or become informed and take a lottery over C^*_H and C''_L , what would they do? It turns out that the value of the test is positive. Even though the test introduces more risk, there is a compensating factor that tips the balance in favor of the lottery. Remaining uninformed entails a real cost; policy C''_U must bear risk to satisfy the high-risk self-selection constraint. Thus, the uninformed will remain so only if the cost of the test is sufficiently high. Accordingly the triplet C^*_H , C''_U , C''_L can only be a Nash equilibrium if there are high testing costs. If the test costs are low, we must consider another possible equilibrium. Suppose insurers expected all the uninformed to take the test, but they could not observe risk status after the test. In that case the only pair satisfying the high-risk self-selection constraint is the Rothschild Stiglitz pair, C^*_H and C^{**}_L . It is fairly straightforward to show that if the uninformed remained so, they would choose C^{**}_L over C^*_H . Thus the choice for the uninformed is to keep C^{**}_L valued without knowledge of risk type or face a lottery between C^*_H (valued with full information of high-risk type) and C^{**}_L (valued with knowledge of low-risk status). It turns out that the value of this lottery is zero. Thus, if the cost of information was zero, and using a tie breaker rule, the uninformed would take the test, and the pair, C^*_H , C^{**}_L is a sequential Nash equilibrium. Regardless of the cost of the test, this cannot be an equilibrium.

We can now summarize. If the costs of information are sufficiently high, there is a sequential equilibrium set C^*_H , C''_U , C''_L . If the information costs are positive but below a threshold, then no sequential Nash equilibrium exists. Finally, there is a knife edge case with an equilibrium of C^*_H , C^{**}_L that exists only with zero cost of information.

Insert Figure 6 here.

Hoel et al. (2006) show that the introduction of heterogeneity about perceived probability of becoming ill in the future makes it possible to circumvent this non-existence of equilibrium. In Hoel et al. (2006), testing is assumed to be costless, but consumers differ with respect to the disutility or anxiety of being informed about future health risk. Using a model with state-dependent utility, the authors assume that some individuals are attracted to chance, while others are repelled by chance. The first are more reluctant to choose testing than the second. Like Doherty and Thistle (1996a), Hoel et al. (2006) conclude that a

regulatory regime in which the use of genetic information by insurers is allowed is better than one in which it is prohibited, but unlike Doherty and Thistle (1996), they obtain that more people undertake the test when test results are verifiable than when they are not. Indeed, in an uncertain but symmetric information setting, when being offered full insurance contracts, some individuals sufficiently repelled by chance choose to take a test. When information is asymmetric with test results being verifiable, untested individuals are offered partial insurance, to dissuade high-risk agents from claiming that they were not tested. By relaxing the verifiability of test results, both (tested) low-risk and untested agents are offered partial insurance to dissuade untested agents from claiming to be low-risk. In contrast to Doherty and Thistle (1996a) who find that all agents choose to be tested when insurers cannot distinguish between untested agents and high-risk agents (for $c = 0$), Hoel et al. (2006) explain why some consumers prefer to stay uninformed even when information on test status is asymmetric.

For other models of insurance purchasing decisions with state dependent utilities, see also Strohmenger and Wambach (2000), who argue that results from standard insurance market models cannot simply be transferred to health insurance markets (due to the assumption that treatment costs are sometimes higher than willingness to pay). State-contingent utilities take into account the fact that people in case of illness have the choice between undergoing treatment or suffering from their disease. Here again, making the results of genetic tests available to the insurer might be welfare improving.

6.4 The case of consent laws

One of the interesting policy applications of this analysis is *consent laws*. Many states have enacted laws governing the disclosure of information from genetic (and other medical) tests. The typical law allows the patient to choose whether to divulge information revealed by the test to an employer or insurer. This issue was considered by Tabarrok (1994), who suggested that consent laws would encourage people to take the test. This was examined further by Doherty and Thistle (1996b), who derived alternative Nash equilibria under consent laws. The principal feature of their analysis is that informed low-risks can verify their low-risk status by presenting the results of the test. Alternatively, informed high-risks will conceal their identity, i.e., withhold consent. This leads to a potential equilibrium containing policies of set $A \equiv \{C_H^*, C_U'', C_L^*\}$ or set $B \equiv \{C_H^*, C_L^*\}$. For B to be an equilibrium, the uninformed must choose to take a diagnostic test when faced with this contract menu. The value of information, $I(B)$, turns out to be positive; this can only be an equilibrium if the information value exceeds the cost of the diagnostic test, c . The other possible equilibrium, A , can hold only if the uninformed remains so. Because the value of information is positive, the equilibrium can only hold if the cost of the test is sufficiently high to discourage testing, $I(A) < c$. Thus, the possible equilibria are A if the

cost of the test is sufficiently high and B if the cost of the test is sufficiently low. There are possible situations where no Nash equilibrium exists or where there are multiple equilibria. Summarizing:

$I(A) < c < I(B)$	two equilibrium sets, A and B
$c < I(A), I(B)$	equilibrium set is B
$I(A), I(B) < c$	equilibrium set is A
$I(A) > c > I(B)$	no Nash equilibrium exists.

In the context of life insurance, Hoy and Polborn (2000) and later Polborn et al. (2006) obtained positive and normative results that are either consistent with or differ from those described in a standard insurance setting. A significant difference is that prohibiting insurance from using information about risk type may increase welfare. In a static setting with initial adverse selection, Hoy and Polborn (2000) argued that genetic testing has a possible dimension for providing positive social value by allowing better-informed consumption choices (while in Doherty and Thistle, the social value of the testing opportunity is negative). The authors constructed three scenarios in which the existence of the test is either Pareto-worsening, Pareto-improving, or is worse off for some consumers and better off for others. The intuition why additional information may lead to a private benefit is as follows. Even if the average equilibrium premium increases as a result of testing, those who are tested (with good or bad news) gain because they can adjust their life insurance demand to their real risk type. In a three-period model, Polborn, Hoy and Sadanand (2006) assumed that people can buy term insurance covering the risk of death either early in life (period 1) before they have received information about their mortality risk and before risk type is known and/or later (period 2) after they have received this information (people face the risk of death only at the beginning of period 3). Here again, if there are sufficiently few individuals who receive bad news about their genetic type, restricting insurers from using information about genetic testing may provide alternative assurances against the risk of classification, in combination with a cap that limits adverse selection.

Empirical studies have dealt with the consequences of a ban on the use of genetic testing in life insurance. Hoy and Witt (2007) provided an economic welfare analysis of the adverse selection costs associated with regulations that ban insurers from access to these tests for the specific case of information relating to breast cancer. These adverse selection costs are shown to be very modest in most circumstances, and the authors argued in favor of restricting the use of genetic test results for rate-making purposes. Using a discrete Markov chain model, Viswanathan et al. (2007) found similar results. They tracked the insurance demand behavior of many cohorts of women who can change their life insurance benefit at the end of each policy year, influenced by the results of tests relating to breast and ovarian cancers (and consequently by their premium changes).

6.5 Moral hazard, public health, and AIDS testing

If the costs and benefits to patients of the potential use of information in insurance markets when consent laws are in place are considered, the value of information is positive, and insurance markets can be encouraged to endorse testing. Whether people actually take medical tests also depends on the costs of those tests. These costs are critical in determining which, if any, Nash equilibrium exists. One can generalize the discussion and talk not only of the costs of the test but also of its other benefits. Quite obviously, testing yields a medical diagnosis that can be useful in treating any revealed condition. In general we would expect this option for treatment to have a positive private and social value (see Doherty and Posey, 1998). Accounting for the private value of this option has the same effect as lowering the cost of the test and tends to favor the equilibrium contract set B , in which all people take the test. However, this opens up the wider issue of other costs and benefits of acquiring information related to risk status.

An interesting twist on this literature concerns the case of AIDS testing. The result that insurance markets tend to raise the private benefit of testing may be reassuring to those interested in public health who normally consider testing for diseases such as AIDS and inherited disorders to be socially beneficial. Several studies have analyzed sexual behavior choices and their effect on the transmission of AIDS and the effectiveness of public health measures (Castillo-Chavez and Hadelar, 1994; and Kremer, 1996). The work of Philipson and Posner (1993) is particularly pertinent: they examined the effect of taking an AIDS test on opportunities to engage in high-risk sexual activity. Without going into detail, the point can be made that people might take the test to verify their uninfected status so they can persuade partners to engage in high-risk sexual activity. Without such an assurance, they might be unable to secure partners for high-risk sex. While this is only one part of their analysis, it is sufficient to illustrate their point that AIDS testing can conceivably *increase* the spread of the disease. They also show that despite the possible social costs of testing, there are private benefits to diagnostic tests because they expand opportunities for sexual trade.

This works tends to tilt the previous analysis of insurance equilibrium, at least for the case of AIDS testing. The insurance equilibrium required a comparison of the costs of testing with the value of (insurance) information revealed by the test. Philipson and Posner (1993) reported an exogenous private benefit of testing. Such a private benefit is the same as lowering the cost of testing. Accordingly, it creates a bias in favor of those equilibria in which all individuals are fully informed of their risk status; i.e., contract set B .

Hoel and Iversen (2002) extended Doherty and Thistle's (1996a) results by taking into account the availability of preventive measures (as private infor-

mation).⁶⁴ In addition to focusing on the regulation of access to information about individual test status,⁶⁵ Hoel and Iversen (2002) took an interest in the possible inefficiencies due to a compulsory/voluntary mix of health insurance.⁶⁶ First, they show that genetic testing and prevention may not be undertaken, even though testing is socially efficient (this inefficiency is likely to occur for systems with a high proportion of compulsory insurance). However, tests may be undertaken when testing is socially inefficient (more likely for systems with substantial voluntary supplementary insurance, and more important the less prevention is).

Finally, while the abovementioned models investigated primary prevention (which reduces the probability of illness), Barigozzi and Henriët (2009) considered a model in which secondary prevention measures (which reduce the health loss when illness occurs) are available. They characterize market outcomes under the four regulatory schemes described by Viswanathan et al. (2007) and derive an unambiguous ranking of these schemes in terms of social welfare. The Disclosure Duty approach weakly dominates all the other regulatory structures. At the other extreme, the Strict Prohibition approach is dominated by all the other regulatory schemes. The Laissez-Faire and the Consent Law approaches appear to be intermediate situations.⁶⁷

7 Concluding remarks: Extensions to the basic models

7.1 Risk categorization and residual adverse selection

Adverse selection can explain the use of risk categorization in insurance markets based on variables that procure information at a low cost (Hoy, 1982; Browne and Kamiya, 2012). For example, in automobile insurance, age and sex variables are significant in explaining probabilities of accidents and insurance premiums (Dionne and Vanasse, 1992; Puelz and Snow, 1994; Chiappori and Salanié, 2000; Dionne et al., 2001, 2006). Particularly, young male drivers (under age 25) are much riskier to insure than the average driver. Because it is almost costless to observe age and sex, an insurer may find it profitable to offer policies with higher premiums to young males. However, this type of categorization is now prohibited in some states and countries. For a survey on adverse selection and

⁶⁴See also Fagart and Fombaron (2003) for a discussion of the value of information under alternative assumptions about what information is available to insurers in a model with preventive measures.

⁶⁵As in Doherty and Thistle (1996b), an individual decides whether or not to obtain the information from testing.

⁶⁶More precisely, voluntary health insurance is considered a supplement to compulsory insurance.

⁶⁷For an empirical study on the impact of insurance on HIV testing, see Sood et al. (2015).

risk classification, see Crocker et al. (2024). On risk classification restrictions, see Dionne and Rothschild (2014).

Dahlby (1983, 1992) provides empirical evidence that adverse selection is present in the Canadian automobile insurance market. He also suggests that his empirical results are in accordance with the Wilson-Miyazaki-Spence model, which allows for cross-subsidization between individuals in each segment defined by a categorization variable such as sex or age: low-coverage policies (low-risks) subsidizing high-coverage policies (high-risks) in each segment.⁶⁸ This important statistical result raises the following question: does statistical categorization enhance efficiency in the presence of adverse selection? In other words, can welfare be improved by using the public information on agents' characteristics (such that age and sex) to offer insurance contracts in the presence of adverse selection? Crocker and Snow (1985, 1986) showed that if the observable variables are correlated with hidden knowledge, costless imperfect categorization always enhances efficiency where efficiency is defined as in Harris and Townsend (1981). Another important contribution in Crocker and Snow (1986) concerns the existence of a balanced-budget tax-subsidy system that provides private incentives to use costless categorization. Note that the corresponding tax is imposed on contracts, not individuals. If a redistribution is made from gains earned on the group in which low-risks are predominant (e.g. old male drivers) to the group in which high-risks are predominant (young male drivers), the classification always permits expansion of the set of feasible contracts. The reason is that the use of categorization relaxes the incentive compatibility constraints. Consequently, with appropriate taxes, no agent loses as a result of categorization. The results are shown for the Wilson-Miyazaki-Spence equilibrium concept but can also sustain an efficient allocation in a Nash equilibrium with a tax system (Crocker and Snow, 1986). These conclusions can be applied to the Wilson anticipatory equilibrium or to the Riley reactive equilibrium, for some values of parameters, both with a tax system. It then becomes clear that prohibiting discrimination for equity considerations imposes efficiency costs in insurance markets (such as automobile insurance, where categorization based on age and sex variables is costless).

Finally, Crocker and Snow (1986) argued that the welfare effects are ambiguous when categorical pricing is costly. In contrast, Rothschild (2011) showed that categorical pricing bans are inefficient even when the categorical pricing technology is costly. In practice, if the government provides breakeven partial social insurance and allows firms to categorize with supplemental contracts, the market will choose to employ categorical pricing only when doing so is Pareto-improving. In other words, providing partial social insurance socializes the provision of the cross-subsidization.

⁶⁸However, Riley (1983) argued that the statistical results of Dahlby (1983) are also consistent with both the Wilson anticipatory equilibrium (1977) and the Riley reactive equilibrium (1979). Both models reject cross-subsidization.

In recent empirical studies, Chiappori and Salanié (2000) and Dionne et al. (2001, 2006) showed that risk classification is efficient to eliminate asymmetric information from an insurer's portfolio, in the sense that there is no residual asymmetric information in the portfolio studied (see Richaudeau, 1999, for an application with a different data set).⁶⁹ They concluded that the insurer was able to control for asymmetric information by using an appropriate risk classification procedure. Consequently, no other self-selection mechanisms inside the risk classes (such as the choice of deductible) are necessary to reduce the impact of asymmetric information, although these are used to justify active underwriting activities by insurers (Browne and Kamiya, 2012). See Chiappori and Salanié (2013) and Dionne (2013) for more detailed analyses of methodologies to isolate information problems in insurance data.

7.2 Multi-dimensional adverse selection

Up to now, it was assumed that risk categories are determined up to the loss probability. However, residual asymmetric information between the insured and the insurers could consist of attitude toward risk. Villeneuve (2003) and Smart (2000) explored the implication of assuming that differences in risk aversion combined with differences in accident probabilities create a multi-dimensional adverse selection problem, where the equilibrium allocation differs qualitatively from the classical results of Rothschild and Stiglitz (1976). In Villeneuve (2003), not only may positive profits be sustainable under several equilibrium concepts (Nash, Rothschild and Stiglitz, Wilson, Riley), but equilibria with random contracts are also possible. The former situation is more likely when low-risk agents are more risk averse, whereas the latter is more likely when low-risks are less risk averse. Villeneuve explored the origin of these phenomena. He gives necessary and sufficient conditions for the comparison of risk aversions that either guarantee or exclude atypical equilibria.

In a companion paper, Smart (2000) obtained similar results. In his model, indifference curves of customers may cross twice; thus the single crossing property does not hold. When differences in risk aversion are sufficiently large, firms cannot use policy deductibles to screen high-risk customers. Types may be pooled in equilibrium or separated by raising premiums above actuarially fair levels. This leads to excessive entry of firms in equilibrium.⁷⁰

Wambach (2000) extended the model of RS by incorporating heterogeneity with respect to privately known initial wealth.⁷¹ He assumes four unobservable

⁶⁹By contrast, Cohen (2005) does not reject residual asymmetric information, with data from Israel.

⁷⁰See also Landsberger and Meilijson (1994) for an analysis of a monopolistic insurer with unobserved differences in risk aversion.

⁷¹Similar conclusions would be obtained if individuals differed in the size of losses (in addition to the difference in risk).

types of individuals: those with high or low risk, with either high or low wealth. When the wealth levels are not too far apart, then types with different wealth but the same risk are pooled, while different risks are separated. The possibility of double-crossing indifference curves occurs for large differences in wealth. In this case, self-selection contracts that earn positive profit might hold in equilibrium. However, in Villeneuve (2003) and Wambach (2000), insurers are restricted to offering only one contract each (in and out of equilibrium).⁷²

Snow (2009) argues that the profitable contracting advanced in these modified Rothschild-Stiglitz environments cannot be sustained as a Nash equilibrium under competitive conditions if insurers are allowed to offer menus of contracts. In the three abovementioned models, the configuration in which the high-risk contract breaks even while the low-risk contract earns a positive profit cannot be a two-stage Nash equilibrium; there always exists a pair of incentive-compatible and jointly profitable contracts attractive to both risk types (an unprofitable contract with full coverage attracting only high-risks and a profitable contract attracting low-risks). Similar reasoning applies to the model investigated by Sonnenholzner and Wambach (2009), combining moral hazard with adverse selection.⁷³

Snow (2009) resolved the problem of non-existence of equilibrium in the related instances by appealing to the three-stage game introduced by Hellwig (1987). When insurers can modify their contractual offers in a third stage of the contracting game, the breakeven pooling contract is the strategically stable Nash equilibrium.

Other studies, including Fluet and Pannequin (1997), Crocker and Snow (2011), and Koehl and Villeneuve (2001), focus on situations where two types of individuals with multiple risks coexist. Fluet and Pannequin (1997) analyze two situations: one where insurers offer comprehensive policies against all sources of risk (complete insurance) and one where different risks are covered by separate policies (incomplete contracts). In the second case, they analyze the possibility that the insurer has perfect information about the coverage of other risks by any insurer in the market. They showed that when market conditions allow for bundling (getting information to protect insurers against undesirable risks), the low-risk individual in a particular market (or for a particular source of risk) does not necessarily buy partial insurance in that market as in the Rothschild and Stiglitz model.

Their analysis emphasizes the trade-off between bundling and spanning. Multiple-risk contracts allow for perfect spanning (taking correlations between

⁷²By contrast, Smart (2000) restricts the entry by a fixed barrier.

⁷³In this model, one case in which profitable self-selection contracting arises, with patient types only partially covered exerting high effort (while impatient types exert low effort and receive lower coverage).

different risks into account) and for perfect bundling (considering all information available to the insurers), while single contracts with imperfect information on contract choice for other risks are inferior because they do not permit risk diversification and information sharing. They show that the former is the more efficient, which confirms the practice used by insurers in many countries.

Unlike Fluet and Pannequin (1997) who considered the possibility of bundling several (independent) risks, Crocker and Snow (2011) decomposed a given risk of loss into its distinct potential causes. The knowledge of the conditional probability of a particular peril occurring is private, as in the model of one-dimensional screening, but applicants signal their type in more than one dimension through the choice of a vector of deductibles. Bundling of coverage for all the perils into a single policy is efficient, like in Fluet and Pannequin (1997) (relative to the solution where the perils were covered by separate contracts) and does not fundamentally alter the structure of screening; high-risks are unaffected by the introduction of multidimensional screening while low-risks obtain more coverage than the high-risks for perils from which they are more likely to suffer. By reducing the externality cost that low-risk agents must bear to distinguish themselves from high-risk agents, multidimensional screening enhances the efficiency of insurance contracting and circumvents the non-existence problem (by decreasing the critical value above which a Nash equilibrium exists).

In the same spirit, Koehl and Villeneuve (2001) considered a multiple-risk environment, but in which exclusivity cannot be enforced and insurers are specialized. The authors compared the profits of the global monopoly and the sum of the profits each monopoly would make in the absence of the other. It is shown that specialization prevents second-best efficiency because it weakens insurers' ability to screen applicants. Even if the market exhibits a form of complementarity that limits the conflict between the insurers (by limiting the conflict between insurers, specialization implicitly sustains collusion between competitors), there are efficiency losses due to specialization, and the profits at the industry level are decreased.

7.3 Symmetric incomplete information and double-sided adverse selection

Some more recent models of multi-period insurance have rejected the presence of initial asymmetries of information and in fact assume the opposite, that information between insurers and insureds is incomplete, but initially symmetric. De Garidel-Thoron (2005) provided a dynamic two-period competitive model in which each agent, together with his initial insurer, learns about his type through accidents. However, other insurers may not, depending on informational structures. In this sense, there is no adverse selection between the policyholder and

his incumbent insurer, but adverse selection may exist between the policyholder and rival insurers.

In fact, these studies have focused on two information structures: symmetric learning and asymmetric learning. Learning is symmetric when the second-period loss probability learned by the incumbent insurer and the policyholder is also observed by rival insurers (this is typically the case when, for example, automobile insurers share accident histories) and asymmetric learning if loss probability is only learned by the current insurer but not by its rivals (when automobile insurers do not share accident histories).

In the absence of ex-ante adverse selection, de Garidel-Thoron (2005) showed that “(i) keeping information about accident claims private is welfare-improving, (ii) such a policy does not jeopardize the existence of an equilibrium, and (iii) this equilibrium exhibits both bonus and malus.” Thus, in a two-period model, adverse selection arises endogenously through differentiated learning about type and leads to a reconsideration of the widespread idea that competition in markets with adverse selection may be undesirable. Indeed, de Garidel-Thoron (2005) showed that it is welfare-enhancing to produce adverse selection of this kind. Moreover, he concluded that the equilibrium contract exhibits lowballing when both parties lack commitment power, but he did not predict the intertemporal pattern (low or highballing) in an environment of one-sided commitment. In the latter context, Jia and Wu (2019) predicted a highballing pattern under mild assumptions on the insurer learning or on consumer preference (HARA utility functions). They concluded that the two opposite predictions (lowballing and highballing) are robust to the presence or absence of adverse selection in period 1 as well as to the symmetric or asymmetric learning hypothesis in period 2 (between the incumbent insurer and its competitors).

In a world of one-sided commitment and symmetric learning, Pauly et al. (1995) developed a model where the coverage of the risk is assumed to be exogenous and showed that, when insurers only engage in price competition, premiums are front-loaded (highballing). This intertemporal pricing pattern will not be overturned by allowing insurers to choose both the premium and the coverage (see Hendel and Lizzeri, 2003; and Pauly et al., 2011). Pauly et al. (2011) further showed that the highballing pricing pattern is robust to the assumption of asymmetric learning.⁷⁴

Other recent models have considered double-sided adverse selection. Seog (2009) formalized a double-sided adverse selection by decomposing the risk of a policyholder into two risks: a general risk and a specific risk. He considers that each party to the insurance contract has superior information; policyholders have superior information about specific risk while insurers have superior information about general risk (for example, policyholders have superior information on their own driving habits, but automobile insurers have superior information about accident risks). High-general-risk consumers are self-insured

⁷⁴See also Cohen (2012) for a model of asymmetric learning among insurers on insured risk.

in equilibrium, while low-general-risk consumers are covered by an insurance contract (full insurance for high-specific-risk people and partial insurance for low-specific-risk people). Consequently, when insurers make their information about general risk public, efficiency is unambiguously improved.

Chassagnon and Villeneuve (2005) and Jeleva and Villeneuve (2004) proposed two extensions of the classical model in which each party knows something that the other does not. Assuming less than perfect risk perception (subjective beliefs), Chassagnon and Villeneuve (2005) characterized the efficient frontier in a competitive setting, while Jeleva and Villeneuve (2004) analyzed the equilibrium between a monopolistic insurer confronted with policyholders having beliefs different from the objective probabilities (the authors formalized this disparity using the Rank Dependent Expected Utility model proposed by Quiggin, 1982, and Yaari, 1987). Both papers find that the optimal offer can be a pooling contract, and that better risks can be better covered.

7.4 Adverse selection and participating contracts

The literature on insurance contract design has focused on non-participating contracts, even if participating contracts are more consistent with Borch's mutualization principle. In non-participating contracts, the premiums are conditioned only on the individual loss (the risk is only transferred to an external risk bearer (stock insurer)), whereas participating contracts condition payout both on the individual loss and the portfolio experience (the premium is subject to a retroactive adjustment or dividend, which depends on the collective loss experience of the pool).

Extending the earlier work of Borch (1962), Marshall (1974) argued that, in the presence of aggregate or social risk and in the absence of adverse selection, mutual insurance is more efficient, unless there are enough independent risks for the law of large numbers to be applied. In the same spirit, Doherty and Dionne (1993) showed how the composite risk transfer implicit in mutual insurance (weakly) dominates the simple risk transfer implicit in stock insurance. They suggested that an efficient insurance contract will decompose risk into diversifiable (or idiosyncratic) and non-diversifiable elements and will let the parties bargain on the sharing of each component.

Smith and Stutzer (1990) introduced adverse selection with undiversifiable aggregate risk. Owing to their participating nature, mutual insurance policies are an efficient risk-sharing mechanism. Smith and Stutzer (1990) show that high-risk policyholders fully insure against both individual and aggregate risk, while low-risk individuals partially insure against both risk types.

Because small mutual insurance firms appear to be less risk sharing, Ligon and Thistle (2005) argued that they must offer their policyholders other advantages, namely, in solving problems of adverse selection. Even in the absence of aggregate risk, their analysis suggests that organization size may be an important component of the institutional structure and provides an alternative explanation for both the existence of mutual insurance firms and the coexistence of stock and mutual insurers. Ligon and Thistle (2005) assumed that even when a risk pool cannot control its composition directly (due to adverse selection), adverse selection can create incentives for the formation of distinct mutual insurers. Adverse selection limits the size of these low-risk mutuals. The combination of stock and mutual insurers is thus shown to solve adverse selection problems by allowing consumers to choose from a menu of contracts.

As in Smith and Stutzer (1990),⁷⁵ high-risk individuals buy conventional fixed-premium policies from stock insurers while low-risk individuals form mutuals. In addition, Ligon and Thistle (1996) derived the conditions⁷⁶ under which stock insurers (for the monopoly and competitive cases) and mutual insurers can coexist, and showed that the mutual can offer higher expected indemnity to low-risk members than the stock insurance policy, without attracting high-risk individuals. Low-risk individuals are strictly better off forming mutuals than buying stock insurance policies. High-risk individuals are no worse off (under monopoly) or are strictly better off (under competition) buying insurance from the stock insurer than joining the mutual. Finally, one empirical implication of their theoretical analysis is that adverse selection may create incentives for some mutuals to be small (while there is no such incentive for stock insurers). Ligon and Thistle (2005) found that the empirical distribution of insurer size by type corresponds precisely with what their theoretical analysis predicts.

More recently, Picard (2014) found that allowing insurers to offer either non-participating or participating policies guarantees the existence of an equilibrium in the Rothschild/Stiglitz model. Participating policies act as an implicit threat that dissuades deviant insurers that would like to attract low-risk agents only (when there is cross-subsidization between risk types) and the WMS allocation can be sustained as a subgame-perfect equilibrium of a non-cooperative game. In other words, an equilibrium holds with high-risk agents having taken out a participating policy subsidized by low-risk individuals because if low-risk agents switch to another insurer, the situation of high-risk agents deteriorates due to the participating nature of their insurance contract. Consequently, it is more difficult for the deviant insurer to attract only low-risk types without attracting high-risk types as well. When there is no equilibrium in the Rothschild/Stiglitz model with non-participating contracts, an equilibrium with

⁷⁵Even if their approach differs from that of Smith and Stutzer (1990) because the problem is one of cooperative game theory.

⁷⁶The conditions under which this separating equilibrium exists are analogous to those under which a separating equilibrium exists in the standard Rothschild/Stiglitz model.

cross-subsidized participating contracts actually exists. Further, this model predicts that the mutual corporate form should be prevalent in insurance lines with cross-subsidization between risk types, while there should be stock insurers in other cases. Picard (2019) generalized the above results in a setting with an arbitrary number of risk types and a more general definition of admissible policy dividend rules. It is also shown that the MWS allocation is the unique equilibrium allocation in this setting under a robustness criterion that rules out equilibria based on arbitrary pessimistic beliefs about non-traded contracts.

In each of these models, the coexistence of stock and mutual insurers occurs either because of exogenous aggregate risk (Doherty and Dionne, 1993; Smith and Stutzer, 1990) or adverse selection (Smith and Stutzer, 1990; Ligon and Thistle, 2005; Picard, 2014). A third explanation for the coexistence of mutual and stock insurers focuses on the possibility of a stock insurer becoming insolvent (i.e., unable to pay all the promised indemnities). Rees et al. (1999) took this possibility into account and assumed that insolvency can be avoided by choosing appropriate capital funds and that agents are fully informed about this choice. In a somewhat similar vein, Fagart et al. (2002) considered that when unbounded losses are possible, insolvency cannot be excluded. The contracts a stock insurer company offers imply a fixed premium that may be negatively adjusted at the end of the contractual period when the losses of stock insurers are too large to be covered by the company's reserves (capital funds and the collected premiums), while the optimal contract offered by a mutual firm involves a systematic ex-post adjustment (negative or positive). These assumptions point to a network effect in insurance (or size effect): the expected utility of an agent insured by a mutual firm is an increasing function of its number of members. For the insurance companies, network externalities also exist but are positive or negative depending on the amount of the capital funds. In an oligopoly game, either one mutual firm or insurance company is active in equilibrium, or a mixed structure emerges in which two or more companies share the market with or without a mutual firm.⁷⁷ Mimra and Wambach (2019b) endogenized the up-front capital of insurers in a competitive insurance market with adverse selection. Under limited liability, low up-front capital gives rise to endogenous insolvency risk, which introduces an externality among customers of an insurer. Mimra and Wambach (2019b) showed that an equilibrium with the MWS allocation always exists. Cream-skimming deviations are unprofitable, as they attract high-risks, who see their expected utility deteriorate if their MWS contract is not cross-subsidized by low-risks and insurer capital is low. Insurers do not have incentives to increase their capital, as this only increases competitors' incentives to cream skim low-risks away from this insurer.

⁷⁷Bourlès (2009) extended this analysis by endogenizing the choice of capital and gave a rationale for mutualization and demutualization waves.

7.5 Adverse selection and non-exclusive contracting

Most of the literature presented so far (implicitly) assumed that exclusive contracting—a consumer trading with only one insurer at a given point in time—is enforceable. However, in many insurance markets, notably life insurance markets, contracting is non-exclusive, with policyholders simultaneously owning policies from multiple insurers without having to inform them of these multiple relationships.⁷⁸

In early work, Jaynes (1978) challenged the standard assumption that contracting is exclusive and allows firms to share information. Jaynes (1978) argued that this results in an equilibrium in which some firms offering the pooling contract preferred by low-risks (Wilson pooling contract) share information among themselves, and some firms that do not share information offer contracts at the actuarially fair high-risk type premium. In other words, all risks buy the pooling contract, and high-risks supplement it with insurance at their actuarially fair premium to reach full insurance. Hellwig (1988) modeled this as the following four-stage game: First, firms offer contracts and can attach an exclusivity condition on it. After that, consumers choose combinations of contracts. In the third stage, insurers decide what customer information to share with what insurers, and in the last stage firms receive information and decide about enforcing exclusivity conditions. Hellwig (1988) showed that the equilibrium allocation proposed in Jaynes (1978) corresponds to a sequential equilibrium of the game. The equilibrium cannot be upset by a cream-skimming offer, as insurers in the last stages can strategically condition information sharing and enforcement of exclusivity conditions on the stage 1 offers they observed. In particular, an insurer offering a cream-skimming contract would not receive information from other firms and hence could not enforce exclusivity conditions. Thus, it cannot prevent high-risk individuals, who would like to supplement their contracts with the attractive low-premium cream-skimming contract, from taking this contract.

Rothschild (2015) analyzed screening in compulsory annuity markets with nonexclusive contracting and linear pricing. Due to non-exclusivity, the classic incentive constraints have to be replaced by "convexification constraints", as the possibility to combine several linear contracts allows buyers to convexify contracts. Rothschild (2015) showed this implies that constrained efficient allocations, which are better for L-types than the pooled fair full-insurance outcome, will be strictly front-loaded for both types, i.e., the H-type allocation does not feature full insurance.

Attar et al. (2014) considered non-exclusive competition in adverse selection markets with convex preferences. The game is a competitive screening game in which firms first simultaneously post arbitrary menus of contracts, from which

⁷⁸We will speak of nonexclusivity when an insurer cannot monitor and therefore not contract on the trades a consumer makes with other insurers.

privately informed consumers then choose in a nonexclusive way. In the insurance model, the unique candidate equilibrium outcome is that the high-risk type obtains full insurance at her actuarially fair price (as in RS), while the low-risk type purchases no insurance, i.e. is excluded.⁷⁹ This is essentially because insurers could pivot on a competitor’s contract that tries to attract the low-risk types with a profit-making contract on H-types. As an example, if the low-risk type RS contract were offered by some insurer, another insurer could offer a contract that makes positive profits on high-risk types and that high-risk types prefer to their fair full insurance contract when purchased *in combination with* the low-risk RS contract. But then, the low-risk type RS contract would be purchased by high-risks and make losses. By similar reasoning, no other positive quantity contract intended for low-risks can be offered in equilibrium.⁸⁰

In Attar et al. (2022), the same authors proposed an insurance market regulation in the basic screening game to overcome this problem and implement the so-called Jaynes (1978)-Hellwig(1988)-Glosten (1994) allocation (JHG). As discussed at the beginning of this section, in the two-type case this allocation has low- and high-risk consumers purchasing the same basic layer of coverage at the fair pooling price (Wilson pooling contract), which high-risk consumers complement by purchasing a complementary layer of coverage at their fair premium. The proposed regulation in Attar et al. (2022) targets firms’ pricing strategies, forbidding them to cross-subsidize between different contracts by engaging in below-cost pricing. This prevents lemon-dropping deviations of the following form: with the possibility of cross-subsidization across contracts, a firm could increase its profit by selling basic coverage to low-risk consumers only, while incurring a small loss by selling complementary coverage to high-risk consumers at slightly better terms than its competitors.⁸¹

Instead of considering regulation, Kosenko et al. (2023) revisited the idea of interfirm communication first discussed in Jaynes (1978) and Hellwig (1988).⁸² Kosenko et al. (2023) analyzed endogenous asymmetric disclosure by firms *and* consumers under non-exclusive contracting. Asymmetric disclosure means that firms and consumers can decide what counterparty they reveal their insurance purchases to. The authors show that the only allocation consistent with a competitive equilibrium is the JHG allocation.⁸³ Asymmetric disclosures, in

⁷⁹In a laboratory experiment on competitive adverse selection markets, Mimra and Waibel (2023) tested and confirmed the theoretical predictions of exclusion of the low type under nonexclusive contracting versus distorted trade of the low type under exclusive contracting.

⁸⁰As in RS, an equilibrium in pure strategies may fail to exist. This is the case if low risks are willing to cross-subsidize high risks for some positive quantity.

⁸¹The problem of high risks wanting to buy multiple copies of the basic layer is addressed by assumptions on preferences in the free entry equilibrium and an assumption on the number of firms providing the basic layer in the oligopoly equilibrium.

⁸²In separate work, Jaynes (2011) also reconsiders strategic communication and allows for communication strategies that are contingent on other firms’ contract offers.

⁸³A competitive equilibrium is defined analogously to Rothschild and Stiglitz (1976) as a set of contracts offered by firms such that no contract results in a negative expected profit, and given the contracts offered by other firms there does not exist any other contract that a firm/entrant can offer which makes positive profits given consumers’s optimal responses to firms’s announced contracts.

the form of insurers revealing information to those firms that the consumer did not reveal as his insurers, ensure that overinsurance by high-risk individuals purchasing the basic layer pooling contracts is prevented on the one hand, and that a deviant firm doesn't have enough information to enforce an exclusive contract that would break the pooling layer.⁸⁴

References

- Abreu, D., Pearce, D. and Stacchetti, E., 1990, "Toward a Theory of Discounted Repeated Games with Imperfect Monitoring," *Econometrica* 58, 1041-1064.
- Akerlof, G.A., 1970, "The Market for 'Lemons' : Quality Uncertainty and the Market Mechanism," *Quarterly Journal of Economics* 84, 488-500.
- Allen, F., 1985, "Repeated Principal-Agent Relationships with Lending and Borrowing," *Economics Letters* 17, 27-31.
- Arnott, R. and Stiglitz, J.E., 1988, "Randomization with Asymmetric Information," *Rand Journal of Economics* 19, 3, 344-362.
- Arrow, K.J., 1963, "Uncertainty and the Welfare Economics of Medical Care," *American Economic Review* 53, 941-969.
- Asheim, G.B. and Nilssen, T., (1996) "Non-discriminating renegotiation in a competitive insurance market". *European Economic Review* 40(9), 1717-1736.
- Attar, A., Mariotti, T. and Salanié, F., 2014, "Nonexclusive Competition under Adverse Selection", *Theoretical Economics*, 9(1), 1-40.
- Attar, A., Mariotti, T. and Salanié, F., 2022, "Regulating Insurance Markets: Multiple Contracting and Adverse Selection", *International Economic Review*, 63(3), 981-1020.
- Azevedo, E., and Gottlieb, D., 2017, "Perfect Competition in Markets With Adverse Selection", *Econometrica* 85(1), 67-105.
- Azevedo, E., and Gottlieb, D., 2019, "An Example of Non-existence of Riley Equilibrium in Markets with Adverse Selection", *Games and Economic Behavior* 116, 152-157.
- Barigozzi, F. and D. Henriët, 2009, "Genetic Information: Comparing Alternative Regulatory Approaches when Prevention Matters", Working Paper, Center For Household, Income, Labour and Demographic Economics.
- Battaglini, M., 2005, "Long-term contracting with Markovian consumers," *American Economic Review*, 95(3) 637-658.
- Bolton, B., 1990, "Renegotiation and the Dynamics of Contract Design," *European Economic Review* 34, 303-310.
- Bond, E.W. and K.J. Crocker, 1991, "Smoking, Skydiving and Knitting: The Endogenous Categorization of Risks in Insurance Markets with Asymmetric Information," *Journal of Political Economy* 99, 177-200.
- Borch, K. (1962) "Equilibrium in a reinsurance market," *Econometrica* 30(3), 424-444.

⁸⁴Lemon-dropping deviations are not relevant in the main analysis as firms offer single contracts, and it is argued in the Appendix that latent contracts can prevent this deviation when firms can offer contract menus.

- Born, P., 2019, "Genetic Testing in Underwriting: Implications for Life Insurance Markets," *Journal of Insurance Regulation*, 38(5), 1-18.
- Bourles, R., 2009, "On the Emergence of Private Insurance in Presence of Mutual Agreements," *Munich Personal RePEc Archive*, Working Paper, 1-30.
- Boyer, M., Dionne, G., and Kihlstrom, R., 1989, "Insurance and the Value of Publicly Available Information" in *Studies in the Economics of Uncertainty in Honour of J. Hadar, T.B. Fomby and T.K. Seo.* (Eds), Springer Verlag, 137-155.
- Browne, M.J. (2006) "Adverse selection in the long-term care insurance market," in Chiappori, P.A. and Gollier, C. (eds), *Competitive failures in insurance markets: theory and policy implications.* MIT Press Book, chapter 5.
- Browne, M.J. and Kamiya, S., 2012, "A Theory of the Demand for Underwriting," *The Journal of Risk and Insurance*, 79, 2, 335-349.
- Caillaud, B., Dionne, G., and Jullien, B., 2000, "Corporate Insurance with Optimal Financial Contracting," *Economic Theory* 16 (1), 77-105.
- Caillaud, B., Guesnerie, R., Rey, P., and Tirole, J., 1988, "Government Intervention in Production and Incentives Theory: A Review of Recent Contributions," *Rand Journal of Economics* 19, 1-26.
- Castillo-Chavez, C. and Hadelor, K.P., 1994, "A Core Group Model of Disease Transmission," Working Paper, Cornell University.
- Chade, H., Schlee, E., 2012, "Optimal Insurance in Adverse Selection," *Theoretical Economics* 7, 571-607.
- Chade, H., Schlee, E., 2020, "Insurance as a Lemons Market: Coverage Denials and Pooling," *Journal of Economic Theory* 189, 105085.
- Chassagnon, A., 1994, "Antisélection et aléa moral dans un modèle principal-agent d'assurance," Mimeo, Chaire d'économie et d'économétrie de l'assurance, EHESS - ENSAE, DELTA.
- Chassagnon, A. and Chiappori, P.A., 1995, "Insurance Under Moral Hazard and Adverse Selection: the Case of Pure Competition," Working Paper, DELTA.
- Chassagnon, A. and Villeneuve, B., 2005, "Efficient Risk Sharing under Adverse Selection and Subjective Risk Perception," *Canadian Journal of Economics* 38, 955-978.
- Chiappori, P. A. and Salanié, B., 2000, "Testing for Asymmetric Information in Insurance Markets," *Journal of Political Economy* 108, 56-78.
- Chiappori, P.A., and Salanié, B., 2013, "Asymmetric Information in Insurance Markets: Predictions and Tests," in G. Dionne (Ed.) *Handbook of Insurance*, Springer, 397-422.
- Chiappori, P.A., Macho, I., Rey, P., and Salanié, B., 1994, "Repeated Moral Hazard: The Role of Memory, Commitment, and the Access to Credit Markets," *European Economic Review* 38, 1527-1553.
- Cho, I. and Kreps, D., 1987, "Signalling Games and Stable Equilibria," *Quarterly Journal of Economics* CII, 179-222.
- Cohen, A., 2005, "Asymmetric Information and Learning: Evidence from the Automobile Insurance Market," *The Review of Economics and Statistics* 87, 197-207.
- Cohen, A., 2012, "Asymmetric Learning in Repeated Contracting: An Empirical Study," *Review of Economics and Statistics* 94, 2, 419-432.

- Cohen, A., and Siegelman, P., 2010, "Testing for Adverse Selection in Insurance Markets," *The Journal of Risk and Insurance* 77, 1, 39-84.
- Cooper, R., 1984, "On Allocative Distortions in Problems of Self-Selection," *Rand Journal of Economics* 15, 4, 568-577.
- Cooper, R. and Hayes, B., 1987, "Multi-period Insurance Contracts," *International Journal of Industrial Organization* 5, 211-231, Reprinted in G. Dionne and S. Harrington (Eds.), *Foundations of Insurance Economics - Readings in Economics and Finance*, Kluwer Academic Publishers, 1992.
- Crocker, K.J. (2023) "The role of normative analysis in markets with hidden knowledge and hidden actions," forthcoming in *The Geneva Risk and Insurance Review*.
- Crocker, K.J. and Snow, A., 1985, "The Efficiency of Competitive Equilibria in Insurance Markets with Adverse Selection," *Journal of Public Economics* 26, 207-219.
- Crocker, K.J. and Snow, A., 1986, "The Efficiency Effects of Categorical Discrimination in the Insurance Industry," *Journal of Political Economy* 94, 321-344, Reprinted in G. Dionne and S. Harrington (Eds.), *Foundations of Insurance Economics - Readings in Economics and Finance*, Kluwer Academic Publishers, 1992.
- Crocker, K.J. and Snow, A., 1992, "The Social Value of Hidden Information in Adverse Selection Economics," *Journal of Public Economics* 48, 317-347.
- Crocker, K.J. and Snow, A., 2008, "Background Risk and the Performance of Insurance Markets under Adverse Selection," *The Geneva Risk and Insurance Review* 33, 1-24.
- Crocker, K.J. and Snow, A., 2011, "Multidimensional Screening in Insurance Markets with Adverse Selection," *The Journal of Risk and Insurance* 78, 2, 287-307.
- Crocker, K.J., Rothschild, C. and Snow, A., 2024, "The Theory of Risk Classification," in this book.
- Cutler D.M., Finkelstein, A., and McGarry, K., 2008, "Preference Heterogeneity and Insurance Markets: Explaining a Puzzle of Insurance", *American Economic Review* 98, 2, 157-162.
- Dahlby, B.G., 1981, "Adverse Selection and Pareto Improvements through Compulsory Insurance," *Public Choice* 37, 547-558.
- Dahlby, B.G., 1983, "Adverse Selection and Statistical Discrimination. An Analysis of Canadian Automobile Insurance," *Journal of Public Economics* 20, 121-130, Reprinted in G. Dionne and S. Harrington (Eds.), *Foundations of Insurance Economics - Readings in Economics and Finance*, Kluwer Academic Publishers, 1992.
- Dahlby, B.G., 1987, "Monopoly Versus Competition in an Insurance Market with Adverse Selection," *Journal of Risk and Insurance* LIV, 325-331.
- Dahlby, B.G., 1992, "Testing for Assymmetric Information in Canadian Automobile Insurance," in *Contributions to Insurance Economics*, G. Dionne (Ed.), Kluwer Academic Publishers.
- D'Arcy, S.P. and Doherty, N., 1990, "Adverse Selection, Private Information and Lowballing in Insurance Markets," *Journal of Business* 63, 145-164.

- Dasgupta, P. and Maskin, E., 1986, "The Existence of Equilibrium in Discontinuous Economic Games, II : Applications," *Review of Economic Studies* 53, 1, 27-41.
- De Donder, P., and Hindriks, J., 2009, "Adverse Selection, Moral Hazard and Propitious Selection", *Journal of Risk and Uncertainty* 38, 1, 73-86.
- De Garidel-Thoron, T., 2005, "Welfare-Improving Asymmetric Information in Dynamic Insurance Markets," *Journal of Political Economy* 113, 121-150.
- De Meza, D. and Webb, D.C., 2001, "Advantageous Selection in Insurance Markets", *Rand Journal of Economics* 32, 2, 249-262.
- Dewatripont, M., 1989, "Renegotiation and Information Revelation over Time : The Case of Optimal Labour Contracts," *Quarterly Journal of Economics* 104, 3, 589-619.
- Diasakos, T. and Koufopoulos, K. 2018, "(Neutrally) Optimal Mechanism under Adverse Selection: The canonical insurance problem", *Games and Economic Behavior* 111,1 59-186.
- Dionne, G., 1983, "Adverse Selection and Repeated Insurance Contracts," *Geneva Papers on Risk and Insurance* 8, 316-333. Reprinted in Dionne and S. Harrington (Eds.), *Foundations of Insurance Economics - Readings in Economics and Finance*, Kluwer Academic Publishers, 1992.
- Dionne, G., 2001, "Insurance Regulation in Other Industrial Countries," in *Deregulating Property-Liability Insurance*, J.D. Cummins (Ed.), Washington: AEI-Brookings Joint Center for Regulatory Studies, Washington, 341-396.
- Dionne, G., 2013, "The Empirical Measure of Information Problems with an Emphasis on Insurance Fraud and Panel Data," in G. Dionne (Ed.) *Handbook of Insurance*, Springer, 423-448.
- Dionne, G. and Doherty, N., 1994, "Adverse Selection, Commitment and Renegotiation with Application to Insurance Markets," *Journal of Political Economy*, 209-235.
- Dionne, G. and Fluet, C., 2000, "Full Pooling in Multi-Period Contracting with Adverse Selection and Noncommitment," *Review of Economic Design* 5, 1, 1-21.
- Dionne, G. and Fombaron, N., 1996, "Non-Convexities and the Efficiency of Equilibria in Insurance Markets with Asymmetric Information," *Economics Letters* 52, 31-40.
- Dionne, G., Fombaron, N., and Doherty, N., 2013a, "Adverse Selection in Insurance Markets" in G. Dionne (Ed.) *Handbook of Insurance*, Springer, 231-280.
- Dionne, G., Gouriéroux, C., and Vanasse, C., 1999, "Evidence of Adverse Selection in Automobile Insurance Markets," in *Automobile Insurance: Road Safety, New Drivers, Risks, Insurance Fraud and Regulation*, G. Dionne and C. Laberge-Nadeau (Eds.), Kluwer Academic Publishers, 13-46.
- Dionne, G., Gouriéroux, C., and Vanasse, C., 2001, "Testing for Evidence of Adverse Selection in the Automobile Insurance Market: A Comment," *Journal of Political Economy* 109, 444-453.
- Dionne, G., Gouriéroux, C., and Vanasse, C., 2006, "The Informational Content of Household Decisions with Applications to Insurance Under Asymmetric

Information," in *Competitive Failures in Insurance Markets*, P.A. Chiappori and C. Gollier (Eds), MIT Press Book, 159-184.

Dionne, G. and Lasserre, P., 1985, "Adverse Selection, Repeated Insurance Contracts and Announcement Strategy," *Review of Economic Studies* 52, 719-723.

Dionne, G. and Lasserre, P., 1987, "Adverse Selection and Finite-Horizon Insurance Contracts," *European Economic Review* 31, 843-862.

Dionne, G. and Lasserre, P., 1988 (revised 1989), "Dealing with Moral Hazard and Adverse Selection Simultaneously," Working Paper, Economics Department, University of Montreal.

Dionne, G., Michaud, P.C., and Dahchour, M., 2013b, "Separating Moral Hazard from Adverse Selection and Learning in Automobile Insurance: Longitudinal Evidence from France," *Journal of the European Economic Association*, 11(4), 897-917.

Dionne, G. and Rothschild, C., 2014, "Economic Effects of Risk Classification Bans," *The Geneva Risk and Insurance Review*, 39, 184-221.

Dionne, G. and Vanasse, C., 1989, "A Generalization of Automobile Insurance Rating Models: The Negative Binomial Distribution with a Regression Component," *Astin Bulletin* 19, 2, 199-212.

Dionne, G. and Vanasse, C., 1992, "Automobile Insurance Ratemaking in the Presence of Asymmetrical Information," *Journal of Applied Econometrics* 7, 149-165.

Doherty, N. and Dionne, G., 1993, "Insurance with Undiversifiable Risk: Contract Structure and Organizational Form of Insurance Firms", *Journal of Risk and Uncertainty* 6, 187-203.

Doherty, N. and Posey, L., 1998, "On the Value of a Checkup: Adverse Selection, Moral Hazard and the Value of Information," *Journal of Risk and Insurance* 65, 189-212.

Doherty, N. and Thistle, P., 1996a, "Adverse Selection with Endogenous Information in Insurance Markets," *Journal of Public Economics* 63, 83-102.

Doherty, N. and Thistle, P., 1996b, "Advice and Consent: HIV Tests, Genetic Tests and the Efficiency of Consent Laws," *Working Paper*, Wharton School, University of Pennsylvania.

Dosis, A., 2022, "Price caps and efficiency in markets with adverse selection" *Journal of Mathematical Economics* 99, 102591.

Durnin, M., Hoy M. and Ruse, M., 2012, "Genetic Testing and Insurance: The Complexity of Adverse Selection", *Ethical Perspectives*, 19(1), 123-154.

Einav, L. and Finkelstein, A., 2011, "Selection in Insurance Markets: Theory and Empirics in Pictures", *Journal of Economic Perspectives* 25(1), 115-138.

Engers, M., and Fernandez, L., 1987. "Market equilibrium with hidden knowledge and self-selection", *Econometrica* 55 (2), 425-439.

Fagart, M.C., 1996, "Concurrence en contrats, anti-sélection et structure d'information," *Annales d'Economie et Statistiques* 43, 1-28.

Fagart, M.C. and Fombaron N., 2003, "Value of Information and Prevention in Insurance", *Working Paper*, Université Paris X Nanterre.

- Fagart, M.C., Fombaron N. and Jeleva, M., 2002, "Risk Mutualization and Competition in Insurance Markets," *Geneva Risk and Insurance Review* 27, 115-141.
- Fang, H., Keane, M.P., and Silverman, D., 2008, "Sources of Advantageous Selection: Evidence from the Medigap Insurance Market," *Journal of Political Economy* 116, 303-350.
- Farinha Luz, V., 2017, "Characterization and uniqueness of equilibrium in competitive insurance," *Theoretical Economics*, 1349-1391.
- Farinha Luz, V., 2022, Optimal dynamic insurance contracts, Working Paper, University of British Columbia.
- Finkelstein, A., McGarry, K.M., and Sufi, A. 2005, "Dynamic Inefficiencies in Insurance Markets: Evidence from Long-Term Care Insurance," *American Economic Review* 95(2), 224-228.
- Finkelstein, A., and McGarry, K.M., 2006, "Multiple Dimensions of Private Information: Evidence of the Long-Term Care Management," *American Economic Review* 96, 938-958.
- Fluet, C., 1992, "Probationary Periods and Time-Dependent Deductibles in Insurance Markets with Adverse Selection" in Contributions to Insurance Economics, G. Dionne (Ed.), Kluwer Academic Publishers.
- Fluet, C. and Pannequin, F., 1997, "Complete Versus Incomplete Insurance Contracts Under Adverse Selection with Multiple Risks," *Geneva Papers on Risk and Insurance Theory* 22, 81-101.
- Fombaron N. and Milcent, C., 2007, "The Distortionary Effect of Health Insurance on Healthcare Demand", Working Paper PSE 40.
- Freixas, X., Guesnerie R. and Tirole, J., 1985, "Planning Under Incomplete Information and the Ratchet Effect," *Review of Economic Studies* 52, 173-191.
- Fudenberg, D., Holmstrom, B. and Milgrom, P., 1986, "Short-term Contracts and Long-term Agency Relationships," Mimeo, University of California, Berkeley.
- Gal, S. and Landsberger, M., 1988, "On 'Small Sample' Properties of Experience Rating Insurance Contracts," *Quarterly Journal of Economics*, 233-243.
- Garella, P., 1989, "Adverse Selection and the Middleman," *Economica* 56, 395-399.
- Gemmo, I., Kubitzka, C., and Rothschild, C., 2020, "Constrained efficient equilibria in selection markets with continuous types," *Journal of Public Economics* 190, 104237.
- Geruso, M. and Layton, T.J., 2017, "Selection in Health Insurance Markets and its Policy Remedies", *Journal of Economic Perspectives* 31(4), 23-50.
- Ghili, S., Handel, B., Hendel, I., and Whinston, M., 2021, "Optimal Long-Term Health Insurance Contracts: Characterization, Computation, and Welfare Effects," *Cowles Foundation Discussion Paper* No. 2218R2.
- Glosten, L.R., 1994, "Is the Electronic Open Limit Order Book Inevitable?" *The Journal of Finance*, 49, 1127-1161.
- Grossman, H.I., 1979, "Adverse Selection, Disassembling, and Competitive Equilibrium," *Bell Journal of Economics* 10, 336-343.

- Guesnerie, R., Picard, P. and Rey, P., 1988, "Adverse Selection and Moral Hazard with Risk Neutral Agents," *European Economic Review* 33, 807-823.
- Handel, B., Hendel, I., and Whinston, M. D. , 2015, "Equilibria in Health Exchanges: Adverse Selection versus Reclassification Risk", *Econometrica*, 83(4), 1261–1313.
- Harris, M. and Townsend, R., 1981, "Resource Allocation under Asymmetric Information," *Econometrica* 49, 33-64.
- Hart, O.D., and Tirole, J., 1988, "Contract Renegotiation and Coasian Dynamics," *Review of Economic Studies* 55, 509-540.
- Hellwig, M.F., 1986, "A Sequential Approach to Modelling Competition in Markets with Adverse Selection," Mimeo, University of Bonn.
- Hellwig, M.F., 1987, "Some Recent Developments in the Theory of Competition in Markets with Adverse Selection," *European Economic Review* 31, 319-325.
- Hellwig, M.F., 1988, "A Note on the Specification of Interfirm Communication in Insurance Markets with Adverse Selection," *Journal of Economic Theory* 46, 154-163.
- Hendel, I. , 2017, "Dynamic Selection and Reclassification Risk: Theory and Empirics". In B. Honoré, A. Pakes, M. Piazzesi, & L. Samuelson (Eds.), *Advances in economics and econometrics: Eleventh world congress* (Econometric Society Monographs, 99–129).
- Hendel, I. and Lizzeri, A. , 2003, "The Role of Commitment in Dynamic Contracts: Evidence from Life Insurance", *Quarterly Journal of Economics*, 118(1), 299–328.
- Hendren, N., 2013, "Private Information and Insurance Rejections" *Econometrica* 81 (5), 1713-1762.
- Hendren, N., 2014, "Unraveling versus Unraveling: A Memo on Competitive Equilibriums and Trade in Insurance Markets", *Geneva Risk and Insurance Review*, 39 (2), 176-183.
- Henriet, D, and Rochet, J.C., 1986, "La logique des systèmes bonus-malus en assurance automobile : une approche théorique," *Annales d'Économie et de Statistique* 1, 133-152.
- Hey, J., 1985, "No Claim Bonus?," *Geneva Papers on Risk and Insurance* 10, 209-228.
- Hoel M., and Iversen, T., 2002, "Genetic Testing When There is a Mix of Compulsory and Voluntary Health Insurance," *Journal of Health Economics* 21, 253-270.
- Hoel M., Iversen, T., Nilssen, T., and Vislie, J., 2006, "Genetic Testing in Competitive Insurance Markets with Repulsion from Chance: A Welfare Analysis," *Journal of Health Economics*, 25, 5, 847-860.
- Hofmann, A. and Browne M., 2013, "One-Sided Commitment in Dynamic Insurance Contracts: Evidence from Private Health Insurance in Germany," *Journal of Risk and Uncertainty* 46: 81-112.
- Hosios, A.J. and Peters, M., 1989, "Repeated Insurance Contracts with Adverse Selection and Limited Commitment," *Quarterly Journal of Economics* CIV, 2, 229-253.

- Hoy, M., 1982, "Categorizing Risks in the Insurance Industry," *Quarterly Journal of Economics* 97, 321-336.
- Hoy, M., 1989, "The Value of Screening Mechanisms Under Alternative Insurance Possibilities," *Journal of Public Economics* 39, 177-206.
- Hoy, M. and Polborn, M., 2000, "The Value of Genetic Information in the Life Insurance Market," *Journal of Public Economics* 78, 3, 235-252.
- Hoy, M. and Witt, J., 2007, "Welfare Effects of Banning Genetic Information in the Life Insurance Market: The Case of BRCA1/2 Genes," *Journal of Risk and Insurance* 3, 523-546.
- Inderst, R. and Wambach, A., 2001, "Competitive Insurance Markets under Adverse Selection and Capacity Constraints," *European Economic Review* 45, 1981-1992.
- Jaynes, G.D., 1978, "Equilibria in Monopolistically Competitive Insurance Markets," *Journal of Economic Theory* 19, 394-422.
- Jaynes, G.D., 2011, "Equilibrium and Strategic Communication in the Adverse Selection Insurance Model" *Working Paper 91*, Yale Economics Department.
- Jeleva, M. and Villeneuve, B., 2004, "Insurance Contracts with Imprecise Probabilities and Adverse Selection," *Economic Theory* 23, 777-794.
- Jia, R. and Wu, Z., 2019, "Insurer Commitment and Dynamic Pricing Pattern", *Geneva Risk and Insurance Review*, 44(1), 87-135.
- Jullien, B., 2000, "Participation Constraints in Adverse Selection Models," *Journal of Economic Theory* 93, 1-47.
- Jullien, B., Salanié B. and Salanié, F., 2007, "Screening Risk Averse Agents under Moral Hazard: Single-Crossing and the CARA Case," *Economic Theory*, 30,), 151-169.
- Koehl, P.E., and Villeneuve, B., 2001, "Complementarity and Substitutability in Multiple-Risk Insurance Markets," *International Economic Review* 42, 245-266.
- Kong, E., Layton, T.J. and Shepard, M., 2023, "Adverse Selection and (Un)natural Monopoly in Insurance Markets", *Working paper*, Harvard University.
- Kosenko, A., Stiglitz, J. and Yun, J., 2023, "Bilateral Information Disclosure in Adverse Selection Markets with Nonexclusive Competition," *Journal of Economic Behavior & Organization*, 205, 144-168.
- Kremer, M., 1996, "Integrating Behavioral Choice into Epidemiological Models of AIDS," *Quarterly Journal of Economics* 111, 549-573.
- Kreps, D., 1989, "Out-of-Equilibrium Beliefs and Out-of-Equilibrium Behaviour," in *The Economics of Information, Missing Markets and Games* (F. Hahn, ed.), Oxford : Clarendon Press, 7-45.
- Kreps, D. and Wilson, R., 1982, "Sequential Equilibria," *Econometrica* 50, 863-894.
- Kunreuther, H. and Pauly, M., 1985, "Market Equilibrium with Private Knowledge : An Insurance Example," *Journal of Public Economics* 26, 269-288. Reprinted in G. Dionne and S. Harrington (Eds.), *Foundations of Insurance*

- Economics - Readings in Economics and Finance, Kluwer Academic Publishers, 1992.
- Lacker, J.M. and Weinberg, J.A., 1999, "Coalition-Proof Allocations in Adverse-Selection Economies," *Geneva Papers on Risk and Insurance Theory* 24, 1, 5-18.
- Laffont, J.J. and Tirole, J., 1986, "Using Cost Observation to Regulate Firms," *Journal of Political Economy* 94, 614-641.
- Laffont, J.J. and Tirole, J., 1987, "Comparative Statics of the Optimal Dynamic Incentive Contracts," *European Economic Review* 31, 901-926.
- Laffont, J.J. and Tirole, J., 1990, "Adverse Selection and Renegotiation in Procurement," *Review of Economic Studies*, 57, 4, 597-625.
- Laffont, J.J. and Tirole, J., 1993, "A Theory of Incentives in Procurement and Regulation," Boston, MIT Press.
- Landsberger, M. and Meilijson, I., 1996, "Extraction of Surplus Under Adverse Selection: The Case of Insurance Markets," *Journal of Economic Theory* 69, 234-239.
- Lemaire, J., 1985, "Automobile Insurance : Actuarial Models," Kluwer-Nighoff Publishing, Boston, 247 pages.
- Levy, Y. and Veiga, A., 2023, "Optimal Contract Regulation in Selection Markets," *Working Paper*.
- Ligon, J.A. and Thistle, P.D., 2005, "The Formation of Mutual Insurers in Markets with Adverse Selection," *Journal of Business* 78, 529-555.
- Lund, D. and Nilssen, T., 2004, "Cream Skimming, Dregs Skimming, and Pooling: On the Dynamics of Competitive Screening," *The Geneva Papers on Risk and Insurance - Theory* 29, 23-41.
- Machina, M.J., 1987, "Choice Under Uncertainty : Problems Solved and Unsolved," *Journal of Economics Perspectives* 1, 121-154. Reprinted in G. Dionne and S. Harrington (Eds.), *Foundations of Insurance Economics - Readings in Economics and Finance*, Kluwer Academic Publishers, 1992.
- Machina, M.J., 2000, "Non-Expected Utility and the Robustness of the Classical Insurance Paradigm," in G. Dionne (Ed.), *Handbook of Insurance*, Kluwer Academic Publishers, 37-96.
- Malueg, D.A., 1986, "Efficient Outcomes in a Repeated Agency Model Without Discounting," *Journal of Mathematical Economics* 15, 217-230.
- Malueg, D.A., 1988, "Repeated Insurance Contracts with Differential Learning," *Review of Economic Studies* LV, 177-181.
- Marshall, J.M., 1974, "Insurance Theory: Reserves versus Mutuality", *Economic Inquiry* 12, 476-92.
- Mimra, W. and Waibel, C., 2023, "Contracting Environments and Efficiency in Markets with Hidden Information: An Experiment", *Working Paper*, ESCP Business School.
- Mimra, W. and Wambach, A., 2016, "A Note on Uniqueness in Game-theoretic Foundations of the Reactive Equilibrium", *Economics Letters* 141, 39-43
- Mimra, W. and Wambach, A., 2019a, "Contract Withdrawals and Equilibrium in Competitive Markets with Adverse Selection" *Economic Theory* 67,

875-907.

Mimra, W. and Wambach, A., 2019b, "Endogenous Insolvency in the Rothschild-Stiglitz Model", *Journal of Risk and Insurance* 86 (1), 165-181.

Miyazaki, H., 1977, "The Rate Race and Internal Labour Markets," *Bell Journal of Economics* 8, 394-418.

Muermann, A. and Rothschild, C., 2014, "New Developments in the Economics of Insurance Markets with Adverse Selection", *The Geneva Risk and Insurance Review* 39,131-135.

Netzer, N. and Scheuer, F., 2014, "A game theoretic foundation of competitive equilibria with adverse selection" *International Economic Review*, 55 (2), 399-422.

Nilssen, T., 2000, "Consumer lock-in with asymmetric information," *International Journal of Industrial Organization* 19, 4, 641-666.

Palfrey, T.R. and Spatt, C.S., 1985, "Repeated Insurance Contracts and Learning," *Rand Journal of Economics* 16, 3, 356-367.

Pannequin, F., 1992, "Théorie de l'assurance et de la sécurité sociale," thèse de doctorat, Université de Paris I.

Pauly, M.V., 1974, "Overinsurance and the Public Provision of Insurance: The Roles of Moral Hazard and Adverse Selection," *Quarterly Journal of Economics* 88, 44-62.

Pauly, M. V., Kunreuther, H., and Hirth, R. A., 1995, "Guaranteed renewability in insurance", *Journal of Risk and Uncertainty*, 143-156.

Pauly, M. V., Menzel, K., Kunreuther, H., and Hirth, R. A. , 2011, "Guaranteed renewability uniquely prevents adverse selection in individual health insurance", *Journal of Risk and Uncertainty*, 43(2), 127-139.

Philipson, T. and Posner, R., 1993, "Private Choice and Public Health: The AIDS Epidemic in an Economic Perspective" Harvard University Press, Cambridge MA.

Picard, P., 1987, "On the Design of Incentives Schemes Under Moral Hazard and Adverse Selection," *Journal of Public Economics* 33, 305-331.

Picard, P., 2014. Participating insurance contracts and the Rothschild Stiglitz equilibrium puzzle. *The Geneva Risk and Insurance Review* 39 (2).

Picard, P., 2019. "Equilibrium in Insurance Markets With Adverse Selection When Insurers Pay Policy Dividends", *The Journal of Risk and Insurance* 86 (4), 887-914.

Polborn M., Hoy, M. and Sadanand, A., 2006, "Advantageous Effects of Regulatory Adverse Selection in the Life Insurance Market", *Economic Journal* 116, 327-354.

Prescott, E. and Townsend, R., 1984, "Pareto Optima and Competitive Equilibria with Adverse Selection and Moral Hazard," *Econometrica* 52, 21-45.

Puelz, R. and Snow, A., 1994, "Evidence of Adverse Selection: Equilibrium Signaling and Cross-Subsidization in the Insurance Market," *Journal of Political Economy* 102, 236-257.

Quiggin, J. (1982), "A theory of anticipated utility," *Journal of Economic Behavior and Organization* 3(4),323-343.

- Radner, R., 1981, "Monitoring Cooperative Agreements in a Repeated Principal-Agent Relationship," *Econometrica* 49, 1127-1148.
- Radner, R., 1985, "Repeated Principal-Agent Games with Discounting," *Econometrica* 53, 1173- 1198.
- Rees, R., Gravelle, H. and Wambach, A., 1999, "Regulation of Insurance Markets", *The Geneva Papers on Risk and Insurance Theory*, 24, 55-68.
- Rey, P. and Salanié, B., 1996, "On the Value of Commitment with Asymmetric Information," *Econometrica* 64, 1395-1414.
- Richaudeau, D., 1999, "Automobile Insurance Contracts and Risk of Accident: An Empirical Test Using French Individual Data," *Geneva Papers on Risk and Insurance Theory* 24, 1, 97-114.
- Riley, J.G., 1979, "Informational Equilibrium," *Econometrica* 47, 331-359.
- Riley, J.G., 1983, "Adverse Selection and Statistical Discrimination : Further Comments," *Journal of Public Economics* 20, 131-137.
- Riley, J.G., 1985, "Competition with Hidden Knowledge," *Journal of Political Economy* 93, 958- 976.
- Rosenthal, R.W. and Weiss, A. (1984) "Mixed-strategy equilibrium in a market with asymmetric information." *The Review of Economic Studies* 51(2),333-342.
- Rothschild, C., 2011, "The Efficiency of Categorical Discrimination in Insurance Markets," *The Journal of Risk and Insurance*, 78, 2,267-285.
- Rothschild, C., 2015, Nonexclusivity, Linear Pricing, and Annuity Market Screening. *Journal of Risk and Insurance*, 82, 1-32.
- Rothschild, C. (2023) "Welfare Analysis in Insurance Markets," forthcoming in *The Geneva Risk and Insurance Review*.
- Rothschild, C., and Thistle, P.D. (2022) "Supply, demand, and selection in insurance markets: Theory and applications in pictures," *Risk Management and Insurance Review* 25(4), 419-444.
- Rothschild, M. and Stiglitz, J., 1976, "Equilibrium in Competitive Insurance Markets : An Essay on the Economics of Imperfect Information," *Quarterly Journal of Economics* 90, 629-650. Reprinted in G. Dionne and S. Harrington (Eds.), *Foundations of Insurance Economics - Readings in Economics and Finance*, Kluwer Academic Publishers, 1992.
- Rothschild, M. and Stiglitz, J., 1997, "Competition and Insurance Twenty Years Later," *Geneva Papers on Risk and Insurance Theory* 22, 73-79.
- Rothschild, C. and Thistle, P.D., 2022, "Supply, Demand, and Selection in Insurance Markets: Theory and Applications in Pictures", *Risk Management and Insurance Review* 25(4), 419-444.
- Rubinstein, A. and Yaari, M., 1983, "Repeated Insurance Contracts and Moral Hazard," *Journal of Economic Theory* 30, 74-97.
- Sabourian, H., 1989, "Repeated Games : A Survey," in the *Economics of Information, Missing Markets and Games* (F. Hahn, Ed.), Oxford : Clarendon Press, 62-105.
- Seog, S.H., 2009, "Insurance Markets With Differential Information", *Journal of Risk and Insurance* 76, 279-294.

- Smart, M., 2000, "Competitive Insurance Markets with Two Unobservables," *International Economic Review* 41, 153-169.
- Smith, B.D., and Stutzer, M.J., 1990, "Adverse Selection, Aggregate Uncertainty, and the Role for Mutual Insurance Contracts," *Journal of Business* 63, 493-510.
- Snow, A., 2009, "On the Possibility of Profitable Self-Selection Contracts in Competitive Insurance Markets," *The Journal of Risk and Insurance* 76, 2, 249-259.
- Sonnenholzner M., and Wambach, A., 2009, "On the Role of Patience in an Insurance Market With Asymmetric Information," *Journal of Risk and Insurance* 76, 2, 323-341.
- Sood, N., Wagner, Z. and Wu, Y., 2015, "The Impact of Insurance on HIV Testing," *American Journal of Health Economics*, 1(4), 515-536.
- Spence, M., 1973, "Job Market Signalling," *Quarterly Journal of Economics* 87, 355-374.
- Spence, M., 1978, "Product Differentiation and Performance in Insurance Markets," *Journal of Public Economics* 10, 427-447.
- Stiglitz, J., 1977, "Monopoly, Nonlinear Pricing, and Imperfect Information: The Insurance Market," *Review of Economic Studies* 44, 407-430.
- Stiglitz, J. and Weiss, A., 1984, "Sorting Out the Differences Between Screening and Signalling Models," Working Paper, Princeton University.
- Strohmenger, R. and Wambach, A., 2000, "Adverse Selection and Categorical Discrimination in the Health Insurance Market: the Effects of Genetic Tests," *Journal of Health Economics* 19, 197-218.
- Tabarrok, A., 1994, "Genetic Testing: An Economic and Contractarian Analysis," *Journal of Health Economics* 13, 75-91.
- Townsend, R., 1982, "Optimal Multiperiod Contracts and the Gain from Enduring Relationships under Private Information," *Journal of Political Economy* 90, 1166-1185.
- Villeneuve, B., 2003, "Concurrence et Antisélection Multidimensionnelle en Assurance," *Annales d'Economie et Statistiques* 69, 119-142.
- Viswanathan, K.S., Lemaire, J., Withers, K., Armstrong, K., Baumritter, A., Hershey, J.C., Pauly, M.V. and Asch, D.A. (2007) "Adverse Selection in Term Life Insurance Purchasing due to the Brca1/2 Genetic Test and Elastic Demand," *The Journal of Risk and Insurance* 74(1), 65-86.
- Wambach, A., 2000, "Introducing Heterogeneity in the Rothschild-Stiglitz Model," *Journal of Risk and Insurance* 67, 579-591.
- Wilson, C., 1977, "A Model of Insurance Markets with Incomplete Information," *Journal of Economic Theory* 16, 167-207.
- Yaari, M.E. (1987) "The Dual Theory of Choice under Risk," *Econometrica* 55(1), 95-115.

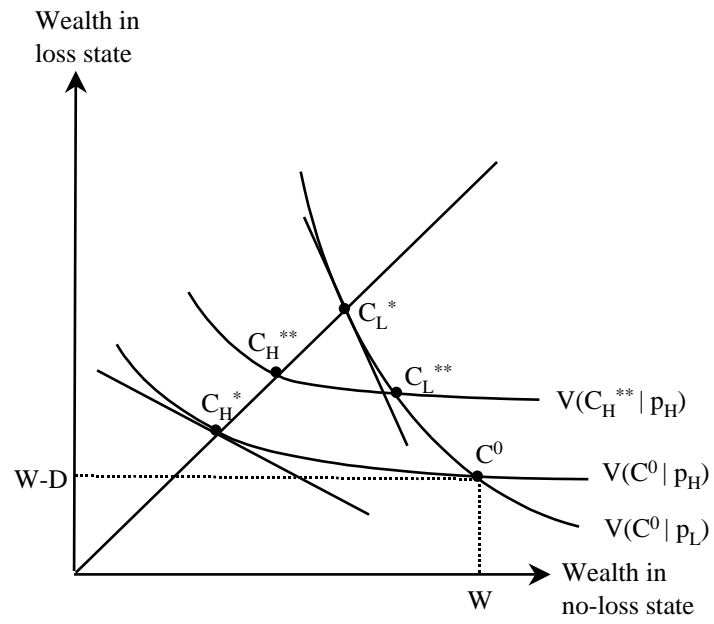


Figure 1: Monopoly model

Expected loss corresponding
to declaration d

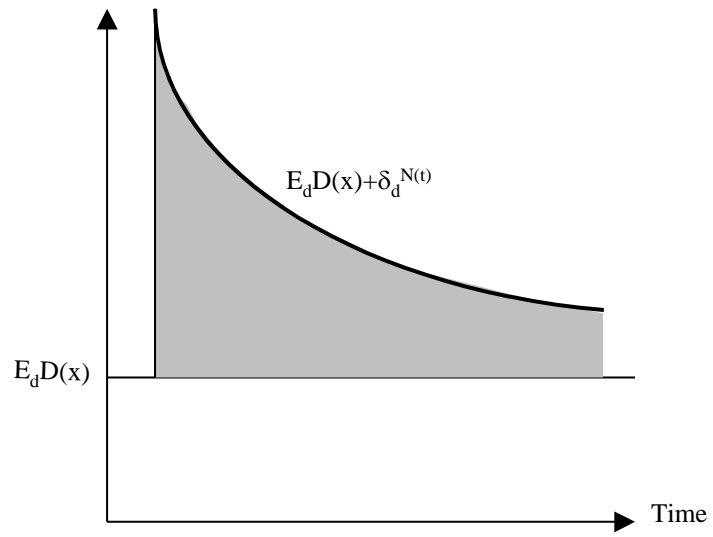


Figure 2: Graphical representation of $E_d D(x) + \delta_d^{N(t)}$

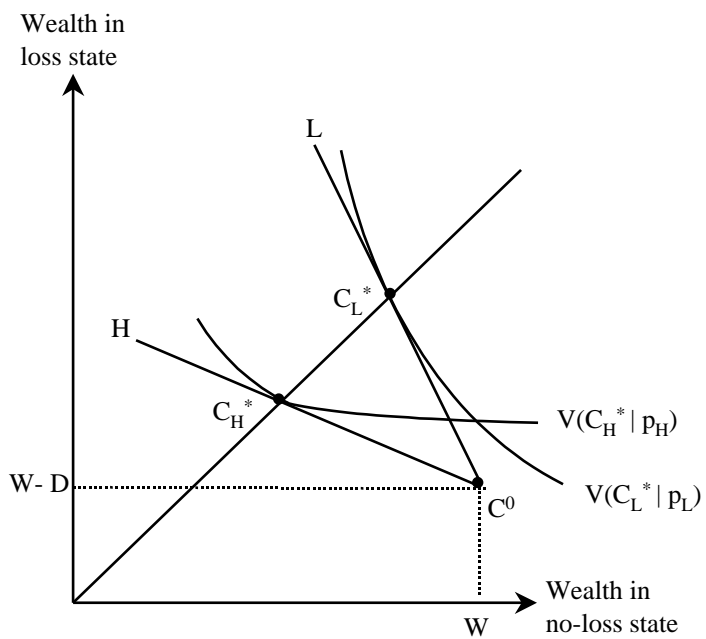


Figure 3: One-period competitive contracts with full information

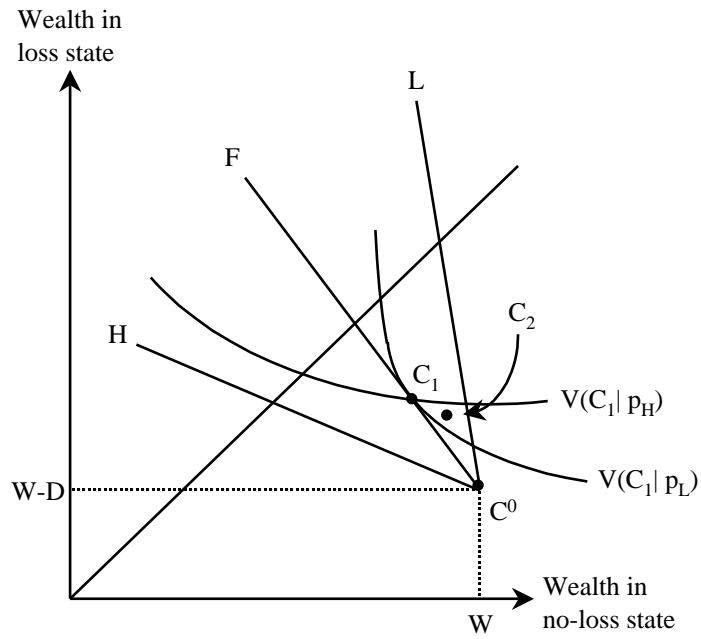


Figure 4a: Inexistence of a Rothschild-Stiglitz pooling equilibrium

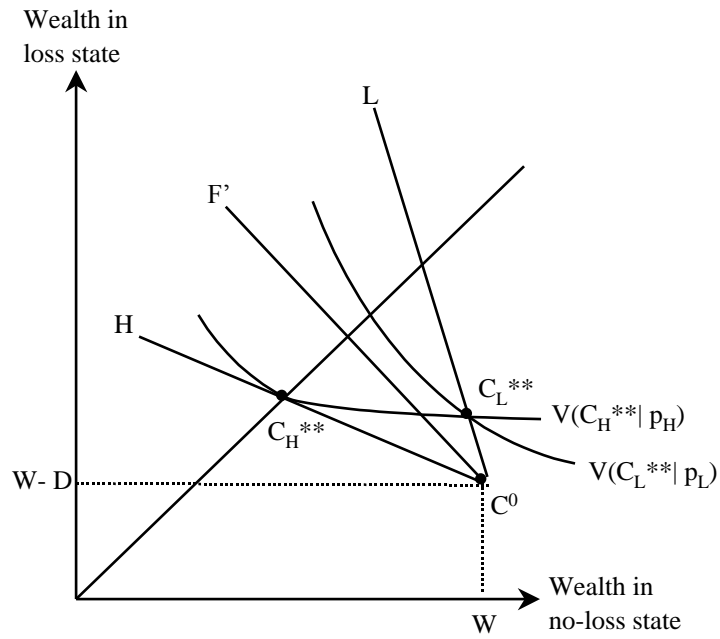


Figure 4b: Existence of a Rothschild and Stiglitz separating equilibrium

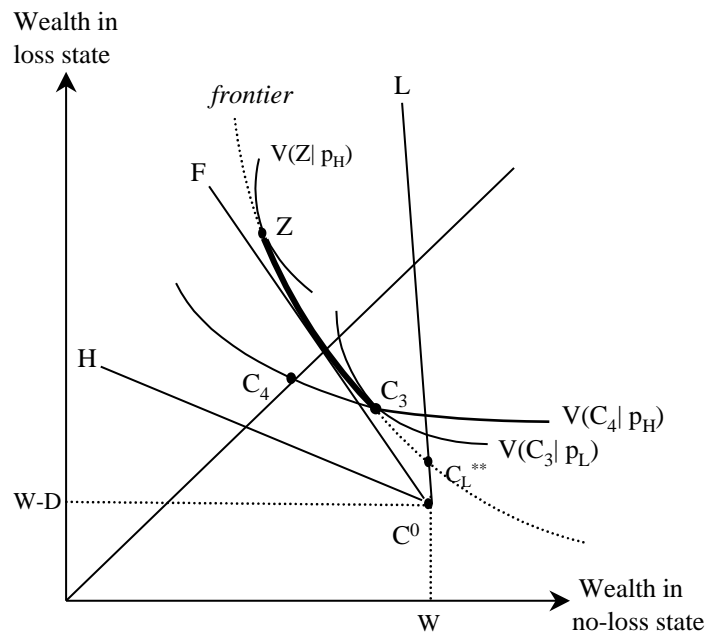


Figure 5: A Wilson-Miyazaki-Spence equilibrium

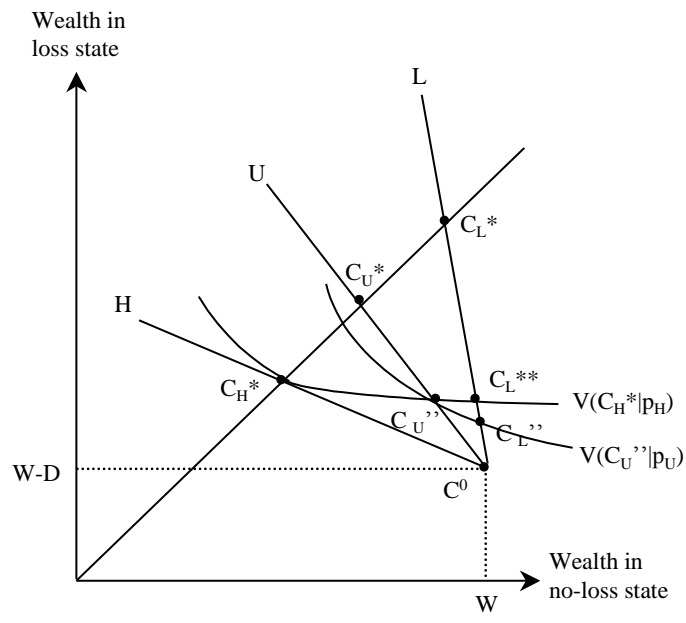


Figure 6: Endogenous information